

Loss aversion or preference imprecision? What drives the WTA-WTP disparity?*

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Abstract

We propose a model that is free of the endowment effect and accounts for the two leading explanations of the disparity between willingness to accept (WTA) and willingness to pay (WTP): loss aversion and preference imprecision. We introduce two axioms that allow us to disentangle how much of the WTA–WTP disparity is attributable to each channel. Our approach is general and encompasses several prominent models as special cases. We further argue that the WTA–WTP gap can be interpreted as a monetary measure of uncertainty aversion. To illustrate our framework, we present a simple experiment in which we decompose the WTA–WTP gap into the contributions of the two channels.

Keywords: willingness to accept, willingness to pay, uncertainty aversion, loss aversion, incomplete preferences, short-selling

JEL classification: D81, D91, C91

1 Introduction

Large observed differences between willingness-to-accept (WTA) and willingness-to-pay (WTP) values (henceforth, gap or disparity) are among the most widely discussed

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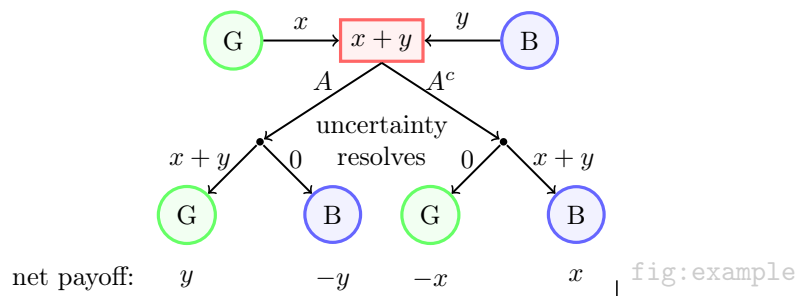
phenomena in behavioral economics. In this paper, we study this disparity for un-
certain prospects, which abound in finance, insurance, sports betting, and gambling
(see, e.g., Horowitz, 2006; Eisenberger and Weber, 1995). The size of the gap in
experiments varies with the design of the study, the elicitation method, and the ex-
act definition. However, the gap is too large to be explained by the standard utility
theory, which ascribes it only to the wealth effects arising from the differences in the
initial positions in WTA and WTP elicitation tasks. (Schmidt and Traub, 2009)

Regarding the behavioural explanation of the gap, the predominant one is based on
the asymmetric treatment of gains and losses: the joy of gaining a prospect is smaller
than the pain of losing it (Kahneman et al., 1991; Marzilli Ericson and Fuster, 2014).
This explanation was recently challenged by Chapman et al. (2023) who found that
the disparity is at most weakly correlated with loss aversion. This observation has
sparked interest in explanations based on preference imprecision or caution (Dubourg
et al., 1994; Cubitt et al., 2015; Cerreia-Vioglio et al., 2015, 2024; Bayrak and Hey,
2020). Despite differences in detail, these explanations share a common intuition:
under uncertainty about relevant tradeoffs, a cautious decision maker (DM) behaves
conservatively, demanding more to sell and offering less to buy.¹ When calibrated
to the data, both explanations of the gap, loss aversion and preference imprecision,
ascribe the entire gap to a single effect. Hence, existing models are not useful for
comparing the relative size of these effects at the aggregate or individual level. We
develop a model in which both effects are present and their strengths can be compared.

In studies on the gap, WTP is elicited in tasks framed as buying a good, while
WTA is usually elicited in tasks framed as selling a pre-owned good. Hence, the two

¹This idea is naturally captured by representing preferences with a set of utility functions rather than a single one. Although Cerreia-Vioglio et al. (2015, 2024) develop complete-preference models, the same underlying set-valued structure also appears in incomplete-preference frameworks (Dubra et al., 2004; Ok et al., 2012 for risk; Galaabaatar and Karni, 2013; Hara and Riella, 2023; Borie, 2023 for uncertainty). The main difference lies in how caution is interpreted. In Cerreia-Vioglio et al. (2015), caution is implemented as a form of pessimism in evaluating acts or certainty equivalents. In incomplete-preference models, caution manifests as inertia (Bewley, 2002): the DM adopts a new option only if it is better under all admissible utilities or beliefs.

Figure 1: There are positions one can take in a gamble: B (blue) and G (green). In position G one is betting x , while in position B one is betting y . If event A (resp. A^c) occurs, position G (resp. B) receives the sum of the bets $x + y$.



tasks differ in terms of the DM's initial endowment. In the classic utility theory, this difference creates an income effect which is the only source of the disparity. In behavioral economics, this idea is further extended as endowment effect: owning a good changes the way one values it. This has led many to view the WTA-WTP gap as equivalent to the endowment effect.² To avoid the difference in the initial endowments, we measure the WTA using *short-selling prices* (not selling prices). Taking a short-selling position in prospect means taking a negative position in that prospect, without owning it.³

Because the payoffs to a buyer and a short-seller are exact opposites while the status quo is identical in both cases, the WTA and WTP elicitation tasks isolate the agent's attitude toward gains and losses, with no endowment effect present. For a discussion of the WTA-WTP disparity under various definitions of buying and selling prices, see Eisenberger and Weber (1995).⁴

Motivating example Consider two positions in a gamble on an uncertain event A

²In models distinguishing these effects, evidence for the endowment effect is weaker than for loss aversion or WTA-WTP disparity (see Plott and Zeiler, 2005 or Marzilli Ericson and Fuster, 2014 for surveys). For example, Brown (2005) found loss aversion not due to the loss of a good, but to the negative net result of buying or selling. Similarly, Shahrabani et al. (2008) found a positive correlation between short-selling price and WTA-WTP disparity. They tested two explanations for the disparity, status quo and endowment effects, and found evidence for the former.

³This way of understanding WTA from the perspective of the organizer rather than the participant of a lottery, common in the literature on risk measures and insurance premiums (Bühlmann, 1970, p.86), is similar to the idea of taking a short position in finance.

⁴See also Lewandowski and Woźny (2022) for a discussion of selling versus short-selling prices.

58 (e.g., whether a favorite team wins an upcoming soccer match), depicted in Figure 1.
59 In position G , one puts x dollars in the pot; in position B , one puts y dollars. If A
60 (resp. A^c) occurs, the person in position G (resp. B) wins the whole pot. Therefore,
61 the net profit of G is y if A occurs and $-x$ otherwise. Since the net profits in G and
62 B are opposite, for a given probability of A , at most one side of the bet may have a
63 positive expected value.

64 If the DM strictly prefers taking either side of a bet to abstaining (i.e., both G
65 and B are strictly preferred to not betting), we call such DM *uncertainty-loving*.
66 Conversely, if the DM rejects at least one side of the bet, we call her *uncertainty-*
67 *averse*. In our framework, a bet may be rejected for two distinct reasons. First, the
68 DM may surely dislike it. Second, the DM may be uncertain about her trade-offs and,
69 out of caution, decline to bet. We call the DM *surely uncertainty-averse* if she strictly
70 dislikes at least one side of every bet. The remaining case, when the DM is unable or
71 unwilling to make a definitive choice, is interpreted as *preference imprecision*.

72 Sure uncertainty aversion (sure UA) is closely related to the idea that losses loom
73 larger than gains. In a bet such as in Figure 1, the two positions always produce
74 exactly opposite net payoffs. When moreover $x = y$ and events A and A^c are sym-
75 metric, swapping positions leaves their attractiveness unchanged, so rejection of one
76 implies rejection of the other for a surely uncertainty-averse DM. Hence our notion of
77 UA extends the classical definition of loss aversion for risk (Kahneman and Tversky,
78 1979), in which individuals reject equal-chance bets involving the same gain and loss.

79 To quantify UA and sure UA, we use the short-selling price (WTA) and the buying
80 price (WTP), along with their extensions proposed by Eisenberger and Weber (1995);
81 Cubitt et al. (2015).⁵

82 Under complete preferences, WTP (resp. WTA) is the indifference price, i.e.,
83 the price at which the DM is indifferent between buying and not buying (or between

⁵Placing a bet can be viewed as a transaction involving the issuance and purchase of a lottery ticket. In the example above, the DM B offers the DM G a ticket paying $x + y$ if A occurs and nothing otherwise, priced at x . The DM G accepts the bet if x does not exceed his WTP, while the DM B is willing to issue the ticket only if x is at least her WTA.

issuing and not issuing) the ticket. Under incomplete preferences, such an indifference price need not exist. We therefore use boundary prices. The buying (resp. short-selling) price is the highest (lowest) price at which the DM prefers the prospect to the status quo. The no-buying (resp. no-short-selling) price is the lowest (highest) price at which the DM is confident that the status quo is preferable. Each pair of boundary prices partitions the price domain into three regions: (i) prices favoring trade, (ii) prices favoring the status quo, and (iii) prices for which the options are incomparable. These boundaries thus convey richer information than a simple buy/not-buy (or short-sell/no-short-sell) choice.

Contribution First, for potentially incomplete preferences over prospects (Savage (1954) acts), we axiomatically define UA. UA, while being weaker than risk aversion, extends some behavioral definitions of loss aversion. Our setting is rich and allows for objective probability, subjective probability, as well as partial or even full ambiguity regarding the underlying probabilities of events. In consequence, our definition differs from many standard definitions of ambiguity/UA in some respects. Our definition uses heading as the benchmark for neutrality rather than subjective expected utility or probabilistically sophisticated preferences (see e.g. Ghirardato and Marinacci, 2002; Epstein, 1999; Schmeidler, 1989).⁶

Second, we distinguish the part of UA that the agent is certain or sure about, and the remaining part due to preference incompleteness. Third, we extend the standard definition of *loss aversion/not loss-loving* of Kahneman and Tversky (1979) from risk and complete preferences to ambiguity and incomplete preferences. Under mild assumptions, we show the equivalence between not loss-loving and UA as well as loss aversion and the sure part of UA.

Fourth, we show how to measure UA, the sure part of UA, and the remaining part attributed to preference incompleteness using counterparts of indifference prices for incomplete preferences. Unlike many standard measures of ambiguity aversion, which

⁶Our notion treats uncertainty in the same way as it treats risk and compares both to certainty, whereas many standard definitions treat uncertainty as something on top of risk.

111 measure the size of the set of subjective beliefs and are unobservable in consequence,
 112 our measures are monetary and can be interpreted as *uncertainty premiums*, i.e., the
 113 amount DM is willing to pay to hedge a given prospect net of its buying price.

114 Fifth, we prove that UA is equivalent to $WTA > WTP$. Thus, we provide an
 115 explanation of the gap. We also define its comparative version (*more uncertainty*
 116 *averse agent and more uncertain prospects*) to argue that the WTA-WTP disparity
 117 is a cardinal measure of UA. We do the same for the sure part of UA. We illustrate
 118 some of our results within the Multi-Utility Multi-Prior (MUMP) model.

119 Sixth, we show how to decompose the WTA-WTP disparity using these mea-
 120 sures: that is, one attributed to loss aversion (i.e. sure UA) and the other attributed
 121 to preferences incompleteness (here interpreted as preference imprecision). This de-
 122 composition allows one to disentangle the two channels that drive the WTA-WTP
 123 disparity. As an illustration, we report the results of an experiment we conducted
 124 to show how our approach can be used to determine which explanation drives the
 125 disparity to a greater extent. We allow people in the elicitation task to express at
 126 which prices they are sure (or unsure) which option, buying (short-selling) or the sta-
 127 tus quo, is better. For this purpose, we adopt the modified multiple price list (MPL)
 128 procedure⁷ proposed by Cubitt et al. (2015) (see also Agranov and Ortoleva, 2025).

129 2 The model and the main results

S:main

130 Let S represent a finite set of states, or, when the context is clear, their total count.
 131 Subsets of S are called events. The outcome set is \mathbb{R} , with elements designating
 132 income amounts. A prospect is a mapping from S to \mathbb{R} , identified with a vector in
 133 \mathbb{R}^S . \mathcal{F} denotes the set of all prospects. We denote by λ ($\in \mathbb{R}$) a constant prospect
 134 whose values are λ for all states. Prospect 0 represents the status quo.

135 Prospects f, g are comonotonic if for all $s, t \in S$, $f(s) > f(t)$ implies $g(s) \geq g(t)$.

⁷The standard MPL procedure is described in Andersen et al. (2006).

136 We say that g is a perfect hedge of f if $f + g = \theta$ for some $\theta \in \mathbb{R}$. We write $f \geq g$ if
137 $f(s) \geq g(s)$ for all $s \in S$, $f > g$ if $f(s) > g(s)$ for all $s \in S$. For a prospect f , we also
138 define $\underline{f} := \min_{s \in S} f(s)$ and $\bar{f} := \max_{s \in S} f(s)$. Given a nonempty event A and real
139 numbers x, y , a prospect f such that $f(A) = x$, $f(A^c) = y$ is called a binary prospect
140 and denoted by $(x, y; A)$. Our setup is that of uncertainty. Risk is a special case
141 where (S, \mathcal{S}, Π) is a probability space, and if the induced probability distributions of
142 two prospects coincide, then the prospects are preferentially equivalent.

143 Let \succsim be a binary relation on \mathcal{F} . For $f, g \in \mathcal{F}$, we say that f and g are *comparable*
144 if $f \succsim g$ or $g \succsim f$, and *incomparable* if neither holds, denoted $f \bowtie g$. The relation
145 \succsim is *complete* if all pairs are comparable. The symmetric and asymmetric parts of \succsim
146 are denoted by \sim and \succ , respectively. If $f \succ 0$, we say that the DM prefers f over
147 the status quo, and in a choice between f and 0 , the DM accepts f . If $f \not\succ 0$, the DM
148 does not prefer f . If $0 \succ f$, the DM strictly dislikes f . If preferences are complete,
149 $f \not\succ g$ is equivalent to $g \succ f$. Under incomplete preferences, $f \not\succ g$ can imply either
150 $g \succ f$ or $g \bowtie f$, reflecting two possible reasons for rejecting f in a choice between
151 f and g : either g is strictly preferred, or f and g are incomparable. We impose the
152 following axioms on \succsim .

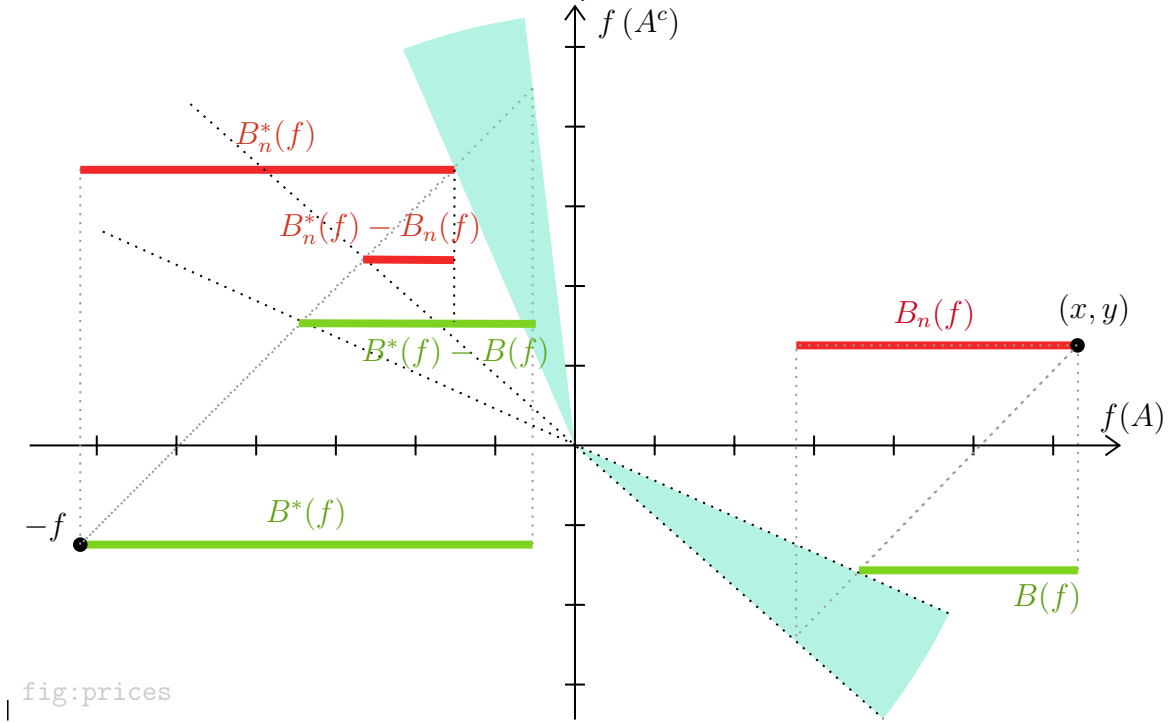
153 **B0 (Preorder)**: \succsim is reflexive and transitive.

154 **B1 (Monotonicity)**: If $f \geq g$ then $f \succsim g$. If, in addition, $f \neq g$, then $f \succ g$.

155 **B2 (Continuity)**: For any $f \in \mathcal{F}$, the sets $nW := \{f \in \mathcal{F} : f \succsim 0\}$ and $nB := \{f \in$
156 $\mathcal{F} : 0 \succsim f\}$ are closed (with respect to the Euclidean topology on \mathbb{R}^S).

157 **B0** and **B1** are standard; **B2** requires closedness, but only for the upper and lower
158 contour sets at 0 ; notably, the corresponding strict contour sets need not be open.

Figure 2: The boundary prices for a binary prospect $(x, y; A)$. The shaded area depicts prospects f for which neither $f \succcurlyeq 0$ nor $0 \succcurlyeq f$. We also illustrate construction of the WTA-WTP gap: $B^*(f) - B^*(f)$ as well as its sure counterpart: $B_n^*(f) - B_n^*(f)$.



2.1 Boundary prices and their basic properties

For prospect $f \in \mathcal{F}$, we define the following four price functionals:

$$\text{buying price } B : \mathcal{F} \rightarrow \mathbb{R} \quad B(f) = \max\{\theta \in \mathbb{R} : f - \theta \succcurlyeq 0\}, \quad (1) \quad \text{Eq:buying2}$$

$$\text{no buying price } B_n : \mathcal{F} \rightarrow \mathbb{R} \quad B_n(f) = \min\{\theta \in \mathbb{R} : 0 \succcurlyeq f - \theta\}, \quad (2) \quad \text{Eq:nobuying2}$$

$$\text{short-selling price } B^* : \mathcal{F} \rightarrow \mathbb{R} \quad B^*(f) = \min\{\theta \in \mathbb{R} : \theta - f \succcurlyeq 0\}, \quad (3) \quad \text{Eq:sellshort2}$$

$$\text{no short-selling price } B_n^* : \mathcal{F} \rightarrow \mathbb{R} \quad B_n^*(f) = \max\{\theta \in \mathbb{R} : 0 \succcurlyeq \theta - f\}. \quad (4) \quad \text{Eq:nosellshort2}$$

The above prices have the following interpretation. The buying price $B(f)$ is the highest price θ at which the DM prefers $f - \theta$ to the status quo. Similarly, the no buying price $B_n(f)$ is the smallest θ at which the DM prefers the status quo to $f - \theta$. $B^*(f)$ and $B_n^*(f)$ are defined analogously, as short-selling and no short-selling prices.

Observe that, in what follows, we use a short-selling price (not a selling price),

when defining the WTA-WTP gap. This allows us to omit the endowment effects resulting from the differences in the initial positions between the buying and selling tasks. Figure 2 depicts the four prices defined for a binary prospect $(x, y; A)$. We state some basic properties of the prices. All proofs are in Section 8.

Lemma 1. *For $X \in \{B, B_n, B^*, B_n^*\}$ and every prospect f , a unique $X(f)$ exists and satisfies the mean property, i.e. $\underline{f} \leq X(f) \leq \bar{f}$. The prices satisfy*

$$B_n(f) \geq B(f), \quad B^*(f) \geq B_n^*(f). \quad (5) \quad \text{1028-1}$$

Moreover, if there is prospect f such that at least one of the inequalities in (5) is strict, then preferences are incomplete.

Prop:CS

Lemma 2. *For any prospect f and any scalar θ , the following holds:*

$$B^*(f) + B(\theta - f) = \theta \quad \text{and} \quad B_n^*(f) + B_n(\theta - f) = \theta. \quad (6) \quad \text{Eq:CS1}$$

Equality (6) is known in the literature as a complementary symmetry between buying and short-selling prices. It has been proven to hold for complete preferences, see Lewandowski and Woźny (2022) for some recent results and the literature discussion. Here, we show that the complementary symmetry holds in settings allowing for incomplete preferences and provide a counterpart of the complementary symmetry between no buying and no short-selling prices.

2.2 Uncertainty aversion and preference imprecision

SS:UA

We define UA and show the WTA-WTP gap measures it.

Definition 1 (UA). *\succsim is **uncertainty averse** if $f \succsim 0$ implies $-f \not\succ 0$ for all $f \in \mathcal{F} \setminus \{0\}$.*

Interpreting the definition, an uncertainty-averse DM will never prefer either side of a bet, i.e., either f or $-f$, to not betting at all. The opposite behavior, where the DM

185 prefers to bet regardless of which side, will be called uncertainty-loving. Intuitively,
 186 UA reflects a dislike for situations where certainty is absent. We now proceed to our
 187 first main result.

188 **Theorem 1.** \succsim is uncertainty averse if and only if $B^*(f) - B(f) > 0$ holds for every
 189 $f \in \mathcal{F} \setminus \{0\}$. ^{prop:UA1}

190 The theorem says that the strictly positive gap between short-selling and buying
 191 prices, the WTA-WTP gap, is equivalent to UA. We also establish the neutrality
 192 benchmark for UA. We say that the DM is *uncertainty neutral* if, for every prospect
 193 f , there exists a unique scalar θ such that $f - \theta \succsim 0$ and $\theta - f \succsim 0$.

194 **Theorem 2.** A DM is uncertainty neutral if and only if $B^*(f) - B(f) = 0 \quad \forall f \in \mathcal{F}$. ^{thm:UAneutralit}

195 **Remark 1** (Uncertainty aversion versus risk aversion). In the risk setting, UA is
 196 weaker than risk aversion at 0. Indeed, for a prospect f with expected value 0, risk
 197 aversion implies $0 \succ f$ and $0 \succ -f$. While such a preference profile is consistent
 198 with UA, it is not necessarily implied by it. ^{Rem:1} Specifically, UA requires that at least one
 199 side of the bet, f or $-f$, is not preferred to the status quo. Thus, it is possible for
 200 an uncertainty-averse DM to accept prospect f while still requiring compensation to
 201 accept the opposite prospect $-f$.⁸ However, UA rules out risk neutrality at 0. For a
 202 prospect f with expected value 0, risk neutrality implies $f \sim 0$ and $-f \sim 0$, meaning
 203 the DM is indifferent between f , $-f$, and the status quo. This preference profile is
 204 not consistent with UA.

205 **Definition 2** (Imprecise preferences). The preferences of a DM are imprecise with
 206 respect to prospect f if there exists $\theta \in \mathbb{R}$ such that $f + \theta \bowtie 0$. Otherwise, the DM's
 207 preferences are precise with respect to prospect f .

⁸Unlike risk aversion, UA allows for the coexistence of gambling and insurance, a behavioral phenomenon discussed since Friedman and Savage, 1948 and Markowitz, 1952. To illustrate, let (x, p) denote a prospect offering a large prize x with small probability p , and nothing otherwise. Many people are willing to pay more than its expected value, i.e., $B(x, p) > xp$, exhibiting risk-loving behavior. At the same time, they may require compensation exceeding the expected value to accept the opposite gamble $(-x, p)$, i.e., $B^*(x, p) > xp$, exhibiting risk-averse behavior. This pattern can coexist under UA whenever $B^*(x, p) > B(x, p) > xp$.

208 Preference imprecision (PI) is a local notion capturing incompleteness of preferences:
 209 if there is a prospect with respect to which the DM is imprecise, we say that her
 210 preferences are incomplete. Otherwise, they are complete.

211 **Theorem 3.** \succsim is imprecise with respect to prospect f if and only if $B_n(f) > B(f)$
 212 and precise if and only if $B_n(f) = B(f)$. Similarly, \succsim is imprecise with respect to
 213 prospect $-f$ if and only if $B^*(f) > B_n^*(f)$ and precise if and only if $B^*(f) = B_n^*(f)$. | prop:imprecise

214 The above theorem shows that the preference imprecision is measured as the gap
 215 between no-buying and buying prices. In fact, for a given prospect, we have two such
 216 measures: $B_n(f) - B(f)$ as well as $B^*(f) - B_n^*(f)$. Generally, the two gaps can differ
 217 (for the same prospect), but later we identify cases for which they are the same.

218 Our aim in the next two parts is to divide UA into that part that stems from
 219 preference imprecision and the remaining part that the DM is sure about.

220 In Subsections 2.3 and 2.4, we define and characterize the notions of *sure UA*
 221 and *strong UA*. These notions then allow us to propose two ways of decomposing the
 222 WTA-WTP gap into sure UA (respectively, strong UA) and preference imprecision.

223 2.3 Sure uncertainty aversion and the decomposition of the 224 WTA-WTP gap

SS:sure

225 **Definition 3** (Sure UA). \succsim is *surely uncertainty averse* if $0 \not\succ f$ then $0 \succ -f$
 226 for all $f \in \mathcal{F} \setminus \{0\}$.

227 Sure UA implies that the status quo must be strictly preferred to at least one side of
 228 any bet. It strengthens the notion of UA.

prop:UA2

229 **Theorem 4.** \succsim is surely uncertainty averse if and only if $B^*(f) - B(f) > 0$ and
 230 $B_n^*(f) - B_n(f) \geq 0$ for every $f \in \mathcal{F} \setminus \{0\}$.

231 Sure UA thus implies the non-negative gap between the no-short selling and no-buying
 232 prices. As the sure UA implies UA, it also means that a short-selling price is strictly

233 larger than a buying price.

234 We now propose our first decomposition of the WTA-WTP gap. Consider an
 235 uncertainty averse DM and some prospect f . By Proposition 4, we have $B^*(f) >$
 236 $B(f)$. By definition of B^* and B , we know that for all θ in between $B(f)$ and $B^*(f)$,
 237 the agent will neither accept $f - \theta$ nor $\theta - f$. We partition this set to capture
 238 two motives (due to indecision or confidence) for why the DM rejects either one of
 239 the two betting positions: $PI_f := \{\theta \in (B(f), B^*(f)) : 0 \not\propto f - \theta\}$, $PI_{-f} := \{\theta \in$
 240 $(B(f), B^*(f)) : 0 \not\propto \theta - f\}$, $\text{sure UA} := \{\theta \in (B(f), B^*(f)) : 0 \succ f - \theta \wedge 0 \succ \theta - f\}$.
 241 By definitions (1)–(4), the size of the above sets can be measured by the respective
 242 boundary prices leading to:

$$\text{decomp 1: } \underbrace{B^*(f) - B(f)}_{\text{UA}} = \underbrace{B^*(f) - B_n^*(f)}_{PI_{-f}} + \underbrace{B_n^*(f) - B_n(f)}_{\text{sure UA}} + \underbrace{B_n(f) - B(f)}_{PI_f} \quad (7)$$

243 This decomposition splits the WTA–WTP gap into three components: one capturing
 244 the *sure* portion of the UA and two capturing preference imprecision with respect to
 245 f and $-f$. The *sure UA* refers to the minimal part of the UA, that is, the portion
 246 that cannot be attributed to preference imprecision. Figure 2 provides a graphical
 247 representation of this decomposition. We now propose an alternative decomposition
 248 that replaces the notion of *sure UA* with that of *strong UA*.

249 2.4 Strong uncertainty aversion and the second decomposition 250 of the WTA-WTP gap

SS:strong

251 Strong UA captures the intuition that if the DM prefers bet f then he must strictly
 252 prefer the status quo to the opposite bet $-f$. This new notion lies in between UA
 253 and sure UA.

254 **Definition 4** (Strong UA). \succ is *strongly uncertainty averse* if $f \succ 0$ implies
 255 $0 \succ -f$ for all $f \in \mathcal{F} \setminus \{0\}$.

Table 1: Preference patterns consistent with the three notions of uncertainty aversion for any nonzero prospect f . + indicates allowed patterns; – indicates ruled-out ones.

f vs. 0	$-f$ vs. 0	UA	strong UA	sure UA
\succsim	\succsim	–	–	–
\succ	\boxtimes	+	–	–
\boxtimes	\succ	+	–	–
\boxtimes	\boxtimes	+	+	–
\prec	$\not\succ$	+	+	+
$\not\succ$	\prec	+	+	+
\prec	\prec	+	+	+

tab:comparisonUA

Theorem 5. \succsim is strongly uncertainty averse if and only if $B^*(f) - B(f) > 0$,
 $B^*(f) - B_n(f) \geq 0$ and $B_n^*(f) - B(f) \geq 0$ for every $f \in \mathcal{F} \setminus \{0\}$.

Note that sure UA implies strong UA and strong UA implies UA – this can be inferred directly, or through the above theorems that also characterize these three notions in terms of boundary prices. Table 1 shows possible patterns of preferences under the three notions of UA.

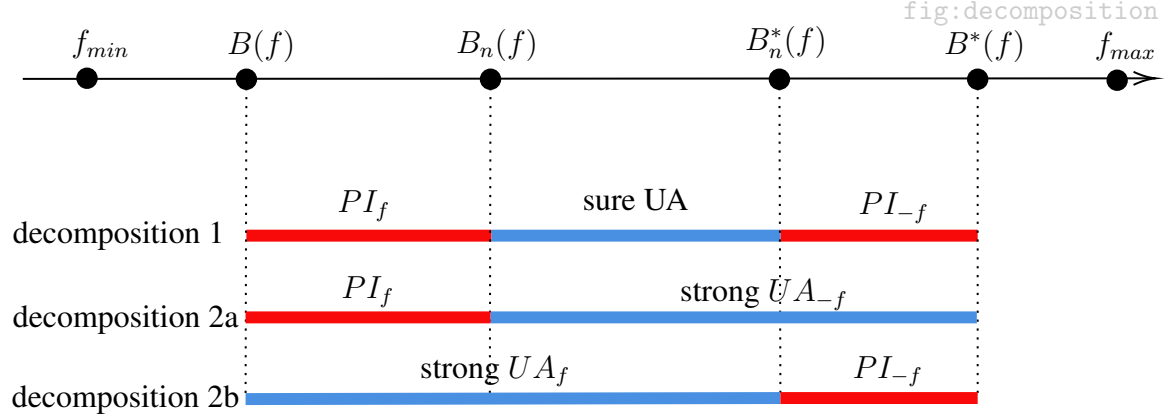
Strong UA leads to the second way we may partition the interval $(B(f), B^*(f))$ for an uncertainty averse individual. Since we have two betting positions, we define two partitions, one for each betting position: $\text{strong UA}_f := \{\theta \in (B(f), B^*(f)) : 0 \succsim f - \theta\}$, $\text{strong UA}_{-f} := \{\theta \in (B(f), B^*(f)) : 0 \succsim \theta - f\}$. This leads to the following two decompositions:

$$\text{decomp 2a:} \quad \underbrace{B^*(f) - B(f)}_{\text{UA}} = \underbrace{B^*(f) - B_n(f)}_{\text{strong UA}_f} + \underbrace{B_n(f) - B(f)}_{\text{PI}_f}. \quad (8)$$

$$\text{decomp 2b:} \quad = \underbrace{B^*(f) - B_n^*(f)}_{\text{PI}_{-f}} + \underbrace{B_n^*(f) - B(f)}_{\text{strong UA}_{-f}}. \quad (9)$$

Figure 3 depicts the three possible decompositions for the case where $B_n^*(f) \geq B_n(f)$. Intuitively, decomposition 1 attributes the smallest part of the WTA-WTP to the (sure) UA, while decompositions 2a and 2b attribute the smallest part of the WTA-WTP to the preference imprecision. See section 5 for examples and illustration.

Figure 3: Uncertainty aversion, measured by the difference between the short-selling price and the buying price of a prospect, is decomposed into preference imprecision (blue) and sure or strong uncertainty aversion (red).



2.5 Binary symmetric prospects

S:Binary

We say that events A and A^c are symmetric for \succsim if, for all $x, y \in \mathbb{R}$, $(x, y; A) \succsim 0 \iff (x, y; A^c) \succsim 0$, and the same implication holds when \succsim is replaced by \precsim .

We say that a binary prospect $(x, y; A)$ is symmetric if the events A and A^c are symmetric.⁹ For such bets, the consequence of Lemma 2 is the following result.

Proposition 1. *For a binary symmetric bet $f = (x, y; A)$, the following holds* prop:equalparts

$$B_n(f) - B(f) = B^*(f) - B_n^*(f).$$

As a result, for a symmetric bet f , the gaps in PI_f and PI_{-f} are identical. This also implies that the strong UA_f and the strong UA_{-f} gaps are the same. These characteristics make binary symmetric prospects particularly useful in applications. We use them in the examples in Section 5, to compare UA with loss aversion for risk in Section 3, and in our experiment reported in Section 6. The intuition behind Proposition 1 is illustrated graphically in Figure 4, where for a binary symmetric bet $f = (x, y; A)$, its perfect hedge is $f^* = (y, x; A)$ (with $\theta = x + y$).

⁹The notion of binary symmetric events generalizes Ramsey's notion of $\frac{1}{2}$ -probability event (see Parmigiani and Inoue, 2009, p.78 or Gul, 1992, Assumption 3).

Figure 4: Due to the symmetry of preferences with respect to the 45° line, all four prices for a binary symmetric prospect f are equal to those for f^* .

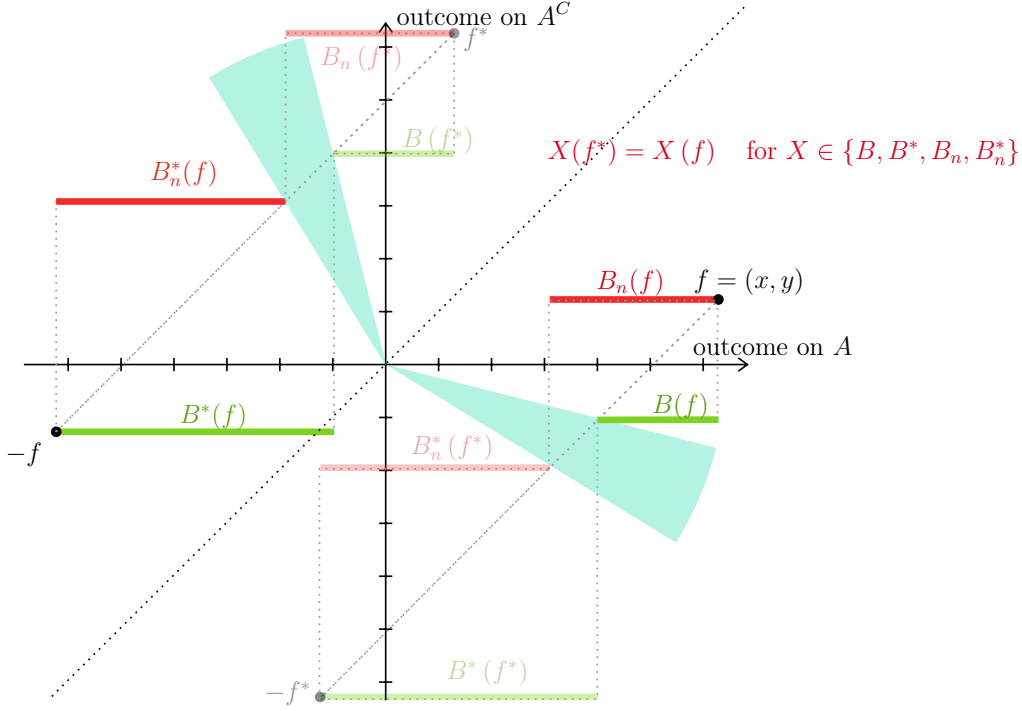


fig:symmetric

3 Uncertainty aversion versus loss aversion

Sse8:lossAversion

Our definition of UA measures the difference between the buying and short selling prices of f , that is, between the price of buying f and the price of buying $-f$. It is hence naturally related to the treatment of gains and losses. We will now establish a formal relationship between UA and loss aversion.

The standard definition of loss aversion for risk (Kahneman and Tversky, 1979) states that a DM dislikes equal-chance gambles of winning or losing the same nonzero amount. In this section, we extend this definition beyond (subjective) probability and beyond complete preferences. We replace equal-chance gambles with binary symmetric prospects. Since \succ generally differs from $\not\prec$ for incomplete preferences, we obtain two definitions instead of one.

Definition 5. \succsim is

(i) **loss averse** (LA) if $0 \succ (x, -x; A)$ holds for every $x \in \mathbb{R} \setminus \{0\}$ and any event

A such that A, A^c are symmetric.

(ii) **not loss-loving** (not-LL) if $(x, -x; A) \not\succeq 0$ for every $x \in \mathbb{R} \setminus \{0\}$ and any event

A such that A, A^c are symmetric.

Remark 2 (Alternative notions of loss aversion). *Kahneman and Tversky (1979) defined loss aversion for risk within prospect theory using the following condition:*

$$x > y \geq 0 \implies (y, -y; 0.5) \succ (x, -x; 0.5), \quad \text{Eq:prospectvalue} \quad (10)$$

where $(x, -x; 0.5)$ denotes a monetary prospect yielding x or $-x$ with equal probability. Under the original version of prospect theory, condition (10) is reflected in the value function being steeper for losses than for gains. Many authors take these properties of the value function, rather than the behavioral condition (10) itself, as the defining feature of loss aversion, thereby anchoring the concept more firmly within specific parametric formulations of prospect theory.¹⁰ Our measure builds directly on the original behavioral condition (10), specifically the case where $y = 0$, and replaces the equal-probability lotteries with symmetric events to suit our ambiguity framework. A stronger version of the condition, allowing $y \neq 0$, is discussed in Remark 3.

We say that the preferences \succsim have *subjective expected utility* (SEU) representation if there exists unique beliefs $\mu \in \Delta(S)$ and a strictly increasing ratio-scale utility $u : \mathbb{R} \rightarrow \mathbb{R}$ with $u(0) = 0$ such that $f \succsim g$ iff $\int_S u(f(s))\mu(ds) \geq \int_S u(g(s))\mu(ds)$.

¹⁰For example Wakker and Tversky (1993) offers a behavioral foundation that leads to the value function being steeper for losses than for gains under cumulative version of prospect theory. Schmidt and Zank (2005) propose an alternative behavioral measure of loss aversion for the original prospect theory. Köbberling and Wakker (2005) define an index of loss aversion as $\lambda = \frac{\lim_{x \rightarrow 0^-} v'(x)}{\lim_{x \rightarrow 0^+} v'(x)}$, based on the local curvature of the value function near the reference point. Abdellaoui et al. (2007) propose a parameter-free method for measuring loss aversion under prospect theory, and Abdellaoui et al. (2016) extend this approach to settings involving ambiguity. More recently, Alaoui and Penta (2025) decompose the utility function under expected utility into two components: one capturing the marginal rate of substitution, and the other reflecting attitudes toward risk and losses.

309 **Proposition 2.** *Assume \succsim have SEU representation with beliefs μ and utility u . Then*
 310 *all of the following are equivalent: UA, sure UA, strong UA, LA, not-LL. Moreover*
 311 *\succsim is uncertainty neutral if and only if u is odd and uncertainty averse if and only if*
 312 *$-u(x) > u(-x)$ holds for all $x \neq 0$.*

313 Clearly, under complete preferences different definitions of UA coincide. The same
 314 is true for loss aversion and not loss-loving. Interestingly, the proposition establishes
 315 that in the class of SEU preferences, UA is equivalent to loss aversion. In particular,
 316 a DM with an odd utility function is uncertainty neutral though not necessarily risk
 317 neutral. For preferences outside SEU, UA is more restrictive than loss aversion.

prop:lossaversion1

318 **Theorem 6.** *The following hold:*

- 319 (i) *If \succsim is uncertainty averse, then it is not loss-loving.*
 320 (ii) *If \succsim is surely uncertainty averse, then it is loss averse.*

321 The reverse implications may not hold in general. Clearly, LA provides restrictions
 322 on preferences for binary symmetric prospects only. This, in general, is too weak
 323 to allow for extensions over arbitrary prospects. However, for preferences defined
 324 over Anscombe–Aumann acts, there exists an additional assumption allowing one to
 325 obtain such an extension and hence imply UA from loss aversion. This assumption
 326 is an incomplete-preferences version of the classical notion of UA due to Schmeidler
 327 (1989). To state it, we extend the set of prospects (only in this section) to $\mathcal{F} = \Delta(X)^S$,
 328 where X is a real interval. A Savage act in this set is represented by an act f
 329 such that for each state s , $f(s) = \delta_x$ for some $x \in \mathbb{R}$. We call such acts purely
 330 subjective. An act f is constant if $f(s) = p$ for any $s \in S$ and some $p \in \Delta(X)$. Given
 331 preferences \succsim over $\Delta(X)^S$, we define preferences over $\Delta(X)$, denoted by $\overline{\succsim}$, as follows:
 332 $p \overline{\succsim} q \iff f \succsim g$, where $f(s) = p$ and $g(s) = q$ for each $s \in S$. We now state an
 333 axiom similar to Schmeidler (1989) UA, but modified to incomplete preferences.

334 **Definition 6** (Schmeidler uncertainty aversion: SUA). *For any two purely subjective*
 335 *acts f, g , if $f \not\succ g$ then $\frac{1}{2}f + \frac{1}{2}g \succ g$.*

336 Under SUA the DM prefers mixing. This allows us to extend loss aversion (not
 337 loss-loving) from binary symmetric prospects to the domain of purely subjective acts.
 Prop:AA

338 **Theorem 7.** *Let \succsim be a preorder on $\Delta(X)^S$.*

339 (i) *If $f(s) \overline{\succ} g(s)$ for all $s \in S$ implies $f \not\succ g$, then SUA and not-LL imply UA.*

340 (ii) *If $f(s) \overline{\succ} g(s)$ for all $s \in S$ implies $f \succ g$, then SUA and LA imply sure UA.*

341 Theorem 7 shows that, under the additional monotonicity condition and Schmeidler
 342 UA, not-LL implies UA, and LA implies sure UA. Combined with Theorem 6, this
 343 yields the equivalence between not-LL and UA, and between LA and sure UA, con-
 344 firming that our notion of UA extends behavioral measures of loss aversion within
 345 this class of preferences. To illustrate Theorem 7 we present the following example.

346 **Example 1.** *Consider a Choquet expected utility model (Schmeidler, 1989) with*
 347 *piecewise-linear utility u (equal to x for gains and λx for losses, $\lambda > 0$) and ca-*
 348 *capacity v . Here, SUA reflects the subadditivity of v , and LA is captured by $\lambda > 1$. For*
 349 *a binary prospect $f = (1, 0; A)$ with $\emptyset \neq A \subset S$, one obtains*

$$B^*(f) - B(f) = 1 - \frac{v(A)}{v(A) + \lambda(1 - v(A))} - \frac{v(A^c)}{v(A^c) + \lambda(1 - v(A^c))}.$$

350 *If $\lambda = 1$ (loss neutrality), the gap reduces to $1 - v(A) - v(A^c)$, the uncertainty-aversion*
 351 *index of Dow and da Costa Werlang (1992) based on SUA. If v is self-conjugate*
 352 *(Schmeidler-uncertainty neutrality), the gap depends only on λ ; for symmetric f , it*
 353 *equals $(\lambda - 1)/(\lambda + 1)$.*

4 WTA-WTP as an uncertainty premium and its comparative statics

S:Measure

In the literature, the WTA–WTP gap is often considered a behavioral phenomenon that should be rationalized by the asymmetric treatment of gains and losses, preference imprecision, caution, or the endowment effect. We now formalize two new interpretations of the WTA–WTP disparity as defined in our paper. Recall that f^* is a perfect hedge of f if $f^* = \theta - f$ for some $\theta \in \mathbb{R}$.

First, consider f and its buying price $B(f)$. By definition, $f - B(f) \succsim 0$, meaning that after purchase the DM faces the prospect $f - B(f)$. Now consider its perfect hedge with $\theta = 0$, that is, $B(f) - f$. By UA, $B(f) - f \not\succsim 0$. This relation implies that some monetary amount must be added to $B(f) - f$ to make it acceptable. Let the smallest such amount be ϵ , so that $\epsilon + B(f) - f \succsim 0$. By definition, $B^*(f) = \epsilon + B(f)$. Hence, the WTA–WTP gap is exactly ϵ , the smallest net amount required to compensate for the uncertainty faced after purchasing f (net of its buying price). In other words, the WTA–WTP gap can be interpreted as an *uncertainty premium* for the individual prospect f itself. Formally, this intuition yields formula (11), a simple consequence of Lemma 2, in the following proposition:

Proposition 3. *For any number θ we have*

$$B^*(f) - B(f) = B^*(f - B(f)), \quad \text{eq:WTA1} \quad (11)$$

$$= \theta - B(\theta - f) - B(f). \quad \text{eq:WTA2} \quad (12)$$

Second, one can also interpret the WTA–WTP gap in terms of perfect hedges. For some sure amount θ , consider f and its perfect hedge $f^* = \theta - f$. Taking each of these prospects individually entails facing uncertainty, but together they remove uncertainty and guarantee θ . The minimal compensations required for f and f^* are captured by the difference between θ and their buying prices. This leads to expression (12), which highlights the WTA–WTP gap as a *premium for the lack of certainty*,

now seen from the perspective of both f and its perfect hedge f^* .

In the remaining subsections, we show the comparative statics results for the uncertainty premium: between individuals, between prospects and between sources of uncertainty. These results further justify WTA-WTP as a monetary measure of UA with the intuitive interpretation as an uncertainty premium.

4.1 More uncertainty averse individual

We start by defining the neutrality benchmark and the across-individual comparison of UA and of sure UA, as captured by the respective price disparities. Formally, let \succsim_i be a preference relation of agent i . Similarly, we denote by $B_i, B_i^*, B_{ni}, B_{ni}^*$ the buying, short-selling, no-buying and no-short-selling price of an individual i , respectively.

Definition 7. \succsim_1 is *more UA* than \succsim_2 if for every $f \in \mathcal{F} \setminus \{0\}$ and some $\epsilon \in \mathbb{R}$:

$$(f \succsim_1 0 \text{ and } \epsilon - f \succsim_1 0) \Rightarrow \exists \delta \in \mathbb{R} : (f - \delta \succsim_2 0 \text{ and } \delta + \epsilon - f \succsim_2 0).$$

\succsim_1 is *more surely UA* than \succsim_2 if for every $f \in \mathcal{F} \setminus \{0\}$ and some $\epsilon \in \mathbb{R}$:

$$(0 \succsim_2 f \text{ and } 0 \succsim_2 \epsilon - f) \Rightarrow \exists \delta \in \mathbb{R} : (0 \succsim_1 f - \delta \text{ and } 0 \succsim_1 \delta + \epsilon - f).$$

Theorem 8. For any $f \in \mathcal{F} \setminus \{0\}$: prop:compUA

(i) \succsim_1 is *more UA* than \succsim_2 iff $B_1^*(f) - B_1(f) \geq B_2^*(f) - B_2(f)$.

(ii) \succsim_1 is *more surely UA* than \succsim_2 iff $B_{n1}^*(f) - B_{n1}(f) \geq B_{n2}^*(f) - B_{n2}(f)$.

Observe that $B_1^*(f)$ is not necessarily higher than $B_2^*(f)$, nor is $B_2(f)$ necessarily higher than $B_1(f)$. This follows directly from the definition, noting that δ need not be positive. A more uncertainty-averse individual will exhibit a larger WTA–WTP gap than a less uncertainty-averse one. The above result together with Theorem 2 suggests a natural way to define UA: a DM is uncertainty-averse if her preferences exhibit more UA than those of an uncertainty-neutral DM. This reinforces that the WTA–WTP gap is an appropriate measure of UA and highlights that its magnitude reflects the degree of UA across individuals. The counterpart to this theorem concerns the measurement of preference imprecision.

401 **Definition 8.** \succsim_1 is *more imprecise wrt* f than \succsim_2 if for every $f \in \mathcal{F} \setminus \{0\}$ and
 402 some $\theta \in \mathbb{R}$: $(f \succsim_1 0 \text{ and } 0 \succsim_1 f + \theta) \Rightarrow \exists \delta \in \mathbb{R} : (f + \delta \succsim_2 0 \text{ and } 0 \succsim_2 f + \delta + \theta)$.

403 **Theorem 9.** For any $f \in \mathcal{F} \setminus \{0\}$, \succsim_1 is more imprecise wrt f than \succsim_2 iff prop:compIP

$$B_{n1}(f) - B_1(f) \geq B_{n2}(f) - B_2(f).$$

404 Lemma 2 implies $B^*(f) = -B(-f)$ and $B_n^*(f) = -B_n(-f)$. Hence an immediate
 405 Corollary to Theorem 9 is that \succsim_1 is more imprecise wrt prospect $-f$ than \succsim_2 iff

$$B_1^*(f) - B_{n1}^*(f) \geq B_2^*(f) - B_{n2}^*(f), \quad \forall f \in \mathcal{F} \setminus \{0\}.$$

406 4.2 More uncertain prospects

407 We now propose a notion of “more uncertain prospects” using only information en-
 408 coded in preferences. Given two prospects f and g , we define g to be *more uncertain*
 409 than f if $g - f$ is a nonconstant prospect comonotonic to f . We say that f (*strongly*)
 410 *uncertainty-dominates* g if g is more uncertain than f and $g - f \not\geq 0$ (respectively,
 411 $g - f \not\leq 0$). Finally, we say that \succsim is *monotonic with respect to (strong) uncertainty-*
 412 *dominance* if $f \succsim g$ whenever f (strongly) uncertainty-dominates g .

Theorem 10. If g is more uncertain than f , then

$$B^*(f) - B(f) \leq B^*(g) - B(g), \quad \text{Eq:1220-3} \quad (13)$$

$$\text{and } B_n^*(f) - B_n(f) \leq B_n^*(g) - B_n(g), \quad \text{Eq:1220-4} \quad (14)$$

413 and this statement is implied by each of the following two sets of conditions: $\text{prop:moreuncertain}$

- 414 (i) \succsim satisfies sure UA and is monotonic with respect to uncertainty-dominance,
- 415 (ii) \succsim satisfies UA and is monotonic with respect to strong uncertainty-dominance.

416 In words, if an agent dislikes prospects that are uncertainty-dominated, the WTA-
 417 WTP gap for such a prospect becomes larger, indicating that the agent demands

a higher uncertainty premium as compensation. Note that uncertainty dominance implies neither $B(f) \geq B(g)$ nor $B^*(f) \leq B^*(g)$. Although such inequalities may hold in particular cases, in general the entire WTA–WTP gap captures the UA.

Remark 3 (A stronger version of loss aversion). *Motivated by the original condition (10) in Kahneman and Tversky (1979), we define a stronger version of loss aversion as follows: for all $x > y \geq 0$ and all events A such that A and A^c are symmetric, $(y, -y; A) \succ (x, -x; A)$. This condition is implied by LA together with the strict version¹¹ of monotonicity with respect to strong uncertainty-dominance. Indeed, fix any event A such that A, A^c are symmetric, any $x > y \geq 0$, and set $\epsilon := x - y > 0$. Then $(y, -y; A)$ is comonotonic with $(\epsilon, -\epsilon; A)$ (with the constant act when $y = 0$ being comonotonic with any act). By LA, $(\epsilon, -\epsilon; A) \prec 0$, hence $(\epsilon, -\epsilon; A) \not\geq 0$. Therefore, $(y, -y; A)$ strongly uncertainty-dominates $(x, -x; A) = (y, -y; A) + (\epsilon, -\epsilon; A)$. By the strict version of monotonicity with respect to strong uncertainty-dominance, we conclude that $(y, -y; A) \succ (x, -x; A)$.*

4.3 The Ellsberg preferences and more uncertain source

Uncertainty dominance captures both hedging behavior and greater variability in outcomes. However, we haven't yet addressed source-dependence (see, e.g., Baillon et al., 2025), one of the crucial aspects of ambiguity. To compare gambles that depend on different sources, we introduce the following property. Formally, a source is an algebra of events. For simplicity, we focus on binary partitions of the state space (E, E^c) , where E is a nonempty proper subset of S and $E^c = S \setminus E$. We say that (E, E^c) dominates (F, F^c) if the following condition holds for all payoffs $x > y$:

$$(x, y; E) \succcurlyeq (x, y; F), \quad \text{and} \quad (x, y; E^c) \succcurlyeq (x, y; F^c). \quad (15)$$

Strict dominance replaces \succcurlyeq with \succ . To illustrate this concept, consider the classic single-urn Ellsberg paradox. An urn contains 30 black balls and 60 red and white balls

¹¹That is, replacing weak with strict preference in the definition.

435 in unknown proportions. A bet on event A pays \$1 if A occurs and \$0 otherwise.
 436 Let event E denote drawing a black ball, and event F denote drawing a red ball.
 437 The standard pattern observed in the Ellsberg experiment consists of a preference for
 438 betting on E over F , and on E^c over F^c . Hence, (E, E^c) dominates (F, F^c) .

P:Source

Theorem 11. *If (E, E^c) dominates (F, F^c) , then*

$$B^*(x, y; E) - B(x, y; E) \leq B^*(x, y; F) - B(x, y; F). \quad \text{Eq:dominance2} \quad (16)$$

Moreover, if at least one of the preferences in (15) is strict, then

$$B^*(x, y; E) - B_n(x, y; E) < B^*(x, y; F) - B(x, y; F). \quad \text{Eq:dominance3} \quad (17)$$

439 Note that if \succsim is precise with respect to the prospects $(x, y; E)$ and $(x, y; E^c)$, then
 440 by Theorem 3 we have $B^* = B_n^*$ and $B = B_n$. Consequently, (17) reduces to a strict
 441 inequality in the WTA–WTP gap. This again highlights that the WTA–WTP gap is
 442 an appropriate measure of UA induced by source preferences.

443 5 WTA–WTP disparity in the MUMP model

S:MUMP

444 We illustrate our results using the multi-utility multi-prior (MUMP) model (see
 445 Galaabaatar and Karni, 2013; Hara and Riella, 2023; Borie, 2023). MUMP is more
 446 specific than our setting, yet general enough to capture preference imprecision and
 447 UA at the same time. We follow Hara and Riella (2023) and assume in this section
 448 that the outcome set is $X = [a, b]$ for some $a, b \in \mathbb{R}$ with $a < 0 < b$ and that all the
 449 discussed properties hold on X rather than on \mathbb{R} .¹²

450 **Definition 9** (MUMP). *\succsim on \mathcal{F} has a MUMP representation if there exist a compact*
 451 *set \mathcal{U} of continuous strictly increasing real-maps on X and a compact convex set Π^u*

¹²MUMP was first formulated in the framework of Anscombe and Aumann (1963), where acts are defined as $\Delta(X)^S$, with $\Delta(X)$ representing the set of probability measures on X and S a finite set of states. In this paper, we restate MUMP within the Savage (1954) framework, using only AA-acts with degenerate lotteries, i.e., Dirac delta measures from $\Delta(X)$.

452 for every $u \in \mathcal{U}$, of probability measures on S such that for each $f, g \in \mathcal{F}$,^{def:MUMP}

$$f \succsim g \iff \int_S u(f) d\mu \geq \int_S u(g) d\mu \quad \text{for every } (\mu, u) \in \Phi. \quad \text{Eq:1112-1} \quad (18)$$

453 where $\Phi = \{(\mu, u) : u \in \mathcal{U}, \mu \in \Pi^u\}$.

454 MUMP contains several important special cases. Single-utility multi-prior (SUMP
455 model of Bewley uncertainty), arises if there is only one utility in the set \mathcal{U} .¹³ Multi-
456 utility single-prior (MUSP) is when the set of priors Π contains only one element
457 and $\Pi^u = \Pi$ for all $u \in \mathcal{U}$. Finally, the case with a single utility and a single prior,
458 corresponds to the Subjective Expected Utility model.

We illustrate our results in the MUMP class. The buying and short-selling prices of f for a “model” $(\mu, u) \in \Phi$, denoted $B_{\mu,u}(f)$ and $B_{\mu,u}^*(f)$, are implicitly defined by

$$\sum_{s \in S} \mu(s) u(f(s) - B_{\mu,u}(f)) = 0, \quad \text{Eq:1030-4} \quad (19)$$

$$\sum_{s \in S} \mu(s) u(B_{\mu,u}^*(f) - f(s)) = 0. \quad \text{Eq:1030-5} \quad (20)$$

Proposition 4. Suppose \succsim has a MUMP representation with the set of priors and utilities Φ . Then for any $f \in \mathcal{F}$, we have^{prop:MUMP}

$$\begin{aligned} B(f) &= \min_{(\mu,u) \in \Phi} B_{\mu,u}(f), & B_n(f) &= \max_{(\mu,u) \in \Phi} B_{\mu,u}(f), \\ B_n^*(f) &= \min_{(\mu,u) \in \Phi} B_{\mu,u}^*(f), & B^*(f) &= \max_{(\mu,u) \in \Phi} B_{\mu,u}^*(f). \end{aligned}$$

459 Proposition 4 shows that under MUMP, the boundary prices correspond to the most
460 optimistic and most pessimistic values across all “models” in Φ . Note that by def-
461 inition, $B(f)$ represents the maximum price the DM is willing to pay for f . Since
462 MUMP requires that $f \succsim 0$ if and only if the subjective expected utility of f exceeds
463 that of 0 for each model in Φ , it follows that $B(f)$ must be the minimum buying
464 price across all models in Φ . A similar interpretation holds for the other three prices.
465 Finally, the gaps between the respective prices (e.g., WTA-WTP) can be interpreted

¹³In the context of buying and short-selling prices, where one alternative is always a deterministic status quo, the SUMP model is equivalent to the two-fold multiplier concordant preferences model of Echenique et al. (2022).

466 as the monetary measure of the size of the set Φ when sampled at prospect f . We
 467 now present two numerical examples. The first illustrates two ways of rationalizing a
 468 given price data set, as well as the distinction between sure and strong UA.

Example 2. Let $f = (10, 0; A)$ be a symmetric prospect, and consider an individual reporting the following indifference prices: $B(f) = 2.39, B_n(f) = 4.05, B_n^*(f) = 5.95, B^*(f) = 7.61$. The two UA decompositions are given by:

$$5.22 \text{ (UA)} = 1.90 \text{ (sure UA)} + 3.32 \text{ (PI}_f + \text{PI}_{-f}) \quad \text{Eq:decomp1} \quad (21)$$

$$5.22 \text{ (UA)} = 3.56 \text{ (strong UA}_f = \text{strong UA}_{-f}) + 1.66 \text{ (PI}_f = \text{PI}_{-f}) \quad \text{Eq:decomp2} \quad (22)$$

Let $a < 0 < b$. We assume that the preference relation \succsim has a MUMP representation with the set of utilities \mathcal{U} and sets of priors Π^u for each $u \in \mathcal{U}$. For given $\alpha, \lambda \in \mathbb{R}_{++}$, the utilities $u_{\alpha, \lambda} : [a, b] \rightarrow \mathbb{R}$ in \mathcal{U} are given by: Ssec:numericalex

$$u_{\alpha, \lambda}(x) = \begin{cases} x^\alpha & \text{for } x \geq 0, \\ -\lambda(-x)^\alpha & \text{for } x < 0. \end{cases}$$

We denote by Π_A^u the set of probabilities $\mu(A)$ for $\mu \in \Pi^u$. For a binary gamble $(x, y; A)$, straightforward calculations yield the indifference prices for each $u \in \mathcal{U}$ and prior $\theta \in \Pi_A^u$:

$$B_{\theta, \alpha, \lambda}(f) = p_{\theta, \alpha, \lambda}x + (1 - p_{\theta, \alpha, \lambda})y, \quad \text{where} \quad p_{\theta, \alpha, \lambda} = \frac{\theta^{1/\alpha}}{\theta^{1/\alpha} + ((1 - \theta)\lambda)^{1/\alpha}},$$

$$B_{\theta, \alpha, \lambda}^*(f) = q_{\theta, \alpha, \lambda}x + (1 - q_{\theta, \alpha, \lambda})y, \quad \text{where} \quad q_{\theta, \alpha, \lambda} = \frac{(\theta\lambda)^{1/\alpha}}{(\theta\lambda)^{1/\alpha} + (1 - \theta)^{1/\alpha}}.$$

469 Note that different θ 's capture preference imprecision in belief, while different α 's
 470 and λ 's capture imprecision in taste. A MUMP model is specified by the set of
 471 triples $(\theta, \lambda, \alpha)$, which defines the utilities and priors in the set Φ . Consider two
 472 such models: $M1$ with $(\theta, \lambda, \alpha) \in \{(0.4, 2.25, 1.05), (0.6, 2.25, 1.05)\}$, and $M2$ with
 473 $(\theta, \lambda, \alpha) \in \{(0.5, 1.50, 1.05), (0.5, 2.25, 0.70)\}$. Note that $M1$ is a SUMP model, while
 474 $M2$ is a MUSP model. The indifference curves of the utilities at 0 in both models are
 475 graphically presented in Figure 5.

Figure 5: Indifference curves of the utilities in Model 1 (left panel) and Model 2 (right panel). The curves show the same UA, strong UA, and sure UA generated either by imprecision in belief or imprecision in taste.

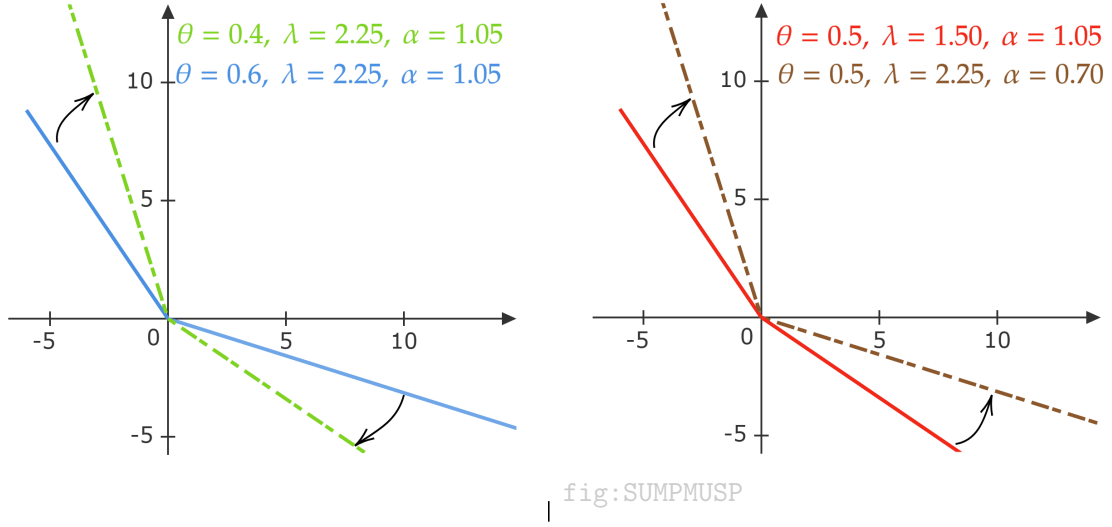


Table 2 shows that in M1, the WTA-WTP gap for each individual utility function is the same, equal to 3.56. In this case, the imprecision is entirely due to uncertainty about the prior, and equals $5.22 - 3.56 = 1.66$, as captured by decomposition (22). In contrast, in M2, the maximal WTA-WTP gap for individual utility functions equals 5.22, capturing the whole UA, while the minimal gap is 1.91, reflecting sure UA. Here, the imprecision is solely due to uncertainty about taste, and equals $5.22 - 1.91 = 3.31$, as captured by decomposition (21). In summary, strong UA is more appropriate for measuring the “sure” part of UA in the SUMP model, while sure UA is more relevant for the MUSP model. Without knowing the true model family, decomposition (21) provides an upper bound on preference imprecision, while decomposition (22) provides a lower bound.

Our second example is a MUSP model with utility functions based on Kőszegi and Rabin (2006) preferences as specified in O’Donoghue and Sprenger (2018). The only source of imprecision is the location of a reference point.

Example 3. Given a reference point $r \in \mathbb{R}$ and two parameters $\eta, \lambda > 0$ let $u(\cdot|r) :$

Table 2: The same UA, sure UA, and strong UA generated in two different models.

model	$(\theta, \lambda, \alpha)$'s	$B_{\theta, \lambda, \alpha}$	$B_{\theta, \lambda, \alpha}^*$	$B_{\theta, \lambda, \alpha}^* - B_{\theta, \lambda, \alpha}$	UA	sure UA	strong UA
M1	(0.4, 2.25, 1.05)	2.39	5.95	<u>3.56</u>	5.22	1.91	<u>3.56</u>
	(0.6, 2.25, 1.05)	4.05	7.61	<u>3.56</u>			
M2	(0.5, 1.50, 1.05)	4.05	5.95	<u>1.91</u>	<u>5.22</u>	<u>1.91</u>	3.56
	(0.5, 2.25, 0.70)	2.39	7.61	<u>5.22</u>			

$\mathbb{R} \rightarrow \mathbb{R}$ be

$$u_r(x) = \begin{cases} x + \eta(x - r) & \text{if } x \geq r, \\ x + \eta\lambda(x - r) & \text{if } x < r. \end{cases}$$

Let $f = (x, y; A)$ be a binary symmetric bet where $x > y$. Let $\eta, \lambda > 0$ be given and $\mu(A) = 0.5$. For $a, b \in \mathbb{R}$ such that $a < b$ we assume that $\mathcal{U} = \{u_r : r \in [a, b]\}$. Buying and short-selling prices of f for an individual utility u_r are given by:

$$B_r(f) = \frac{x + y + \eta(x - r) + \eta\lambda(y - r)}{2 + \eta + \eta\lambda} + \begin{cases} \frac{2\eta r}{2 + \eta + \eta\lambda} & \text{if } r < 0, \\ \frac{2\eta\lambda r}{2 + \eta + \eta\lambda} & \text{if } r \geq 0. \end{cases}$$

$$B_r^*(f) = \frac{x + y + \eta(y + r) + \eta\lambda(x + r)}{2 + \eta + \eta\lambda} - \begin{cases} \frac{2\eta r}{2 + \eta + \eta\lambda} & \text{if } r < 0, \\ \frac{2\eta\lambda r}{2 + \eta + \eta\lambda} & \text{if } r \geq 0. \end{cases}$$

We consider WTA and WTP as functions of r for $x = 200$, $y = -50$, $\eta = 2$, $\lambda = 2$ and $r \in [-50, 100]$. We thus have $B_r(f) = 43.75 + 0.25|r|$, $B_r^*(f) = 106.25 - 0.25|r|$, and $B^*(f) - B(f) = \max_{r \in [-50, 100]} [B_r^*(f) - B_r(f)] = B_0^*(f) - B_0(f) = 62.5$, $B_n^*(f) - B_n(f) = \min_{r \in [-50, 100]} [B_r^*(f) - B_r(f)] = B_{100}^*(f) - B_{100}(f) = 12.5$. Hence, the entire gap of 62.5 is divided into sure UA (12.5) and preference imprecision (50).

6 Experimental illustration

S:Experiment

Method We elicited buying, no-buying, short-selling, and no-short-selling prices for risky and ambiguous prospects using a multiple price list (MPL). Each MPL offered three response options for every prospect price (row): “I certainly would buy” (left), “I am not sure” (middle), and “I certainly would not buy” (right). A rational subject

500 should buy at low prices and refrain at high prices, possibly expressing uncertainty
501 in between. The row where a participant first switches from the left to either of the
502 other two options defines the range of buying prices; the row where she first switches
503 to the right from either of the other two defines the range of no-buying prices.¹⁴

504 Short-selling and no-short-selling prices are elicited analogously, except that the
505 rational switching direction is reversed: the subject receives the sure amount for
506 issuing a lottery ticket. Thus a rational subject should short-sell at high prices and
507 refrain at low prices. Participants received training on MPLs and correctly answered
508 comprehension questions before each survey.

509 **Prospects** Each prospect involved drawing a ball at random from an urn containing
510 90 balls, each either red and yielding the higher payoff, or blue and yielding the lower
511 payoff. There were two *payoff pairs*, (600, 100) and (400, 300), and three *sources*
512 of uncertainty, represented by different levels of information about the urn: *RISK*,
513 where half the balls are red and half blue; *UNCERTAINTY*, where the composition
514 is unknown; and *PARTIAL*, where 30 balls are blue, 30 red, and 30 of unknown color.

515 **Design** Subjects were randomly assigned to one of three groups differing in the
516 prospects to be evaluated: (a) source: *RISK*, payoff pairs: (600, 100), (400, 300); (b)
517 source: *UNCERTAINTY*, payoff pairs: (600, 100), (400, 300); (c) sources: *RISK*,
518 *PARTIAL*, *UNCERTAINTY*, payoff pair: (600, 100). Each subject received two
519 MPLs per prospect: one to elicit buying and no-buying prices and one to elicit short-
520 selling and no-short-selling prices. The full instructions, MPL tables, and compre-
521 hension quiz are provided in the Supplementary materials.

522 **Subjects and data** Ninety-two bachelor and master’s students, aged 19–33, from
523 the SGH Warsaw School of Economics participated. Participation was voluntary and
524 unpaid. The experiment was not incentivized (see the discussion in the last section
525 on the challenges of designing incentives for this class of experiments). We collected

¹⁴We use the midpoint of these ranges to identify buying and no-buying prices (and analogously short-selling and no-short-selling prices); results are similar when using minimum or maximum values.

207 and, after removing incomplete ones, 170 respondent–prospect observations.

Results Figure 6 presents the decompositions for prospects with payoffs (600, 100). The upper panel displays the sure UA decomposition; the lower panel shows the mean of the two strong UA decompositions, which were very similar.

We identify four groups of individuals (separated by dashed vertical lines): (1) A group for which the entire gap consists of sure/strong UA (positive or negative); (2) A group for which both components of the decomposition are strictly positive; (3) A group for which the entire gap is due to imprecision; (4) A group for which the sure/strong component is negative (uncertainty loving). In the fourth group, the overall UA gap may be positive or negative depending on whether positive imprecision outweighs negative sure/strong UA.

7 Discussion and concluding remarks

S:Discuss

Correlation between WTA and WTP and between the WTA-WTP gap and loss aversion Recently, Chapman et al. (2023) showed that WTA and WTP are not correlated and that the disparity between them is only weakly correlated with loss aversion. This challenges the view that loss aversion is the main explanation for the WTA–WTP disparity. We re-examine their findings using our dataset, our measure of WTA, and our measure of loss aversion. The left panel of Figure 7 shows the relation between WTA and WTP, and the right panel shows the relation between the WTA–WTP disparity and loss aversion. While we replicate their finding of no correlation between WTA and WTP, we document a positive correlation between the WTA–WTP gap (UA) and our measure of loss aversion (sure UA).

Cautious expected utility Cerreia-Vioglio et al. (2024) propose an explanation of the WTA–WTP gap based on caution. Their approach differs from ours in several respects. First, they discuss the WTA–WTP disparity in the context of the endowment

Figure 6: Absolute decomposition of UA (i.e., the WTA-WTP gap). Each vertical segment represents one individual. The upper panel presents decomposition 1. The bottom panel presents the mean of decomposition 2a and 2b. An absolute part of the UA attributed to preference imprecision is presented in orange (always positive), while the sure or strong part of the gap is presented in blue. Respondents are ordered by UA (black line), separately within four groups (explained in main text). The upper panel clipped at 600.

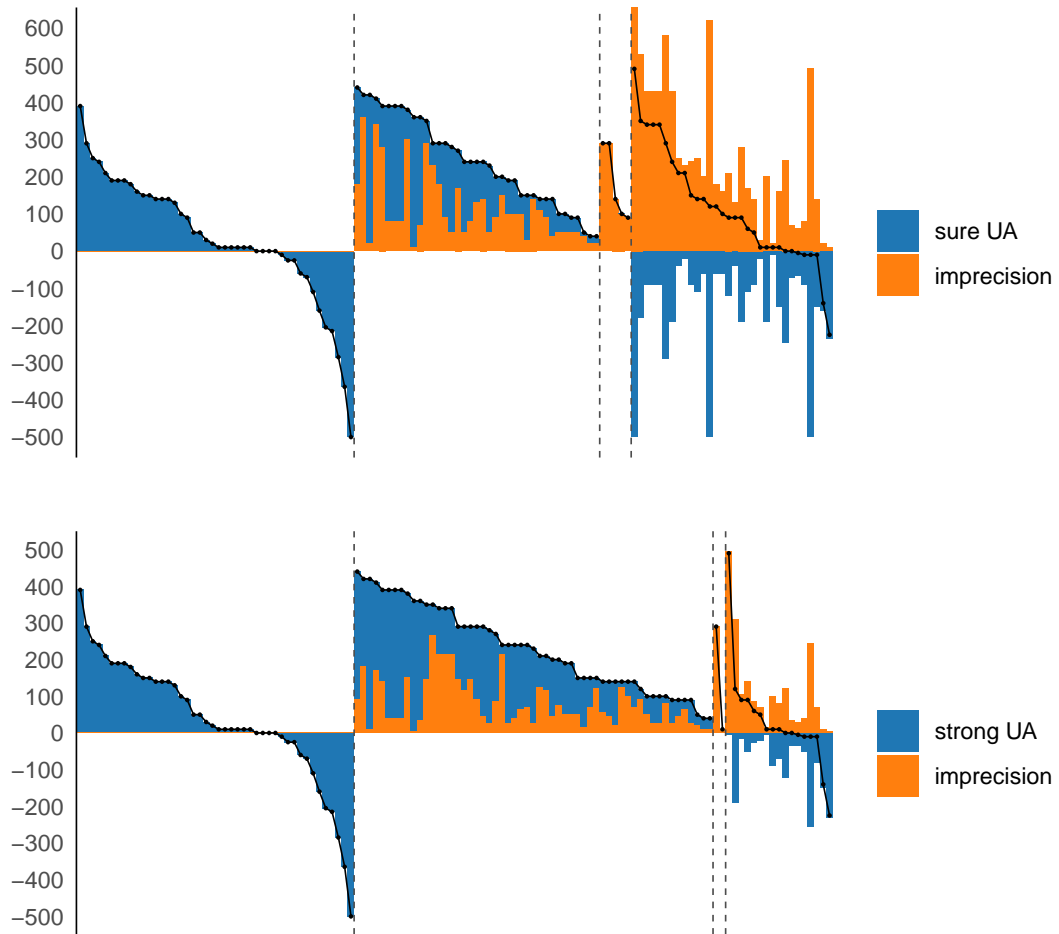
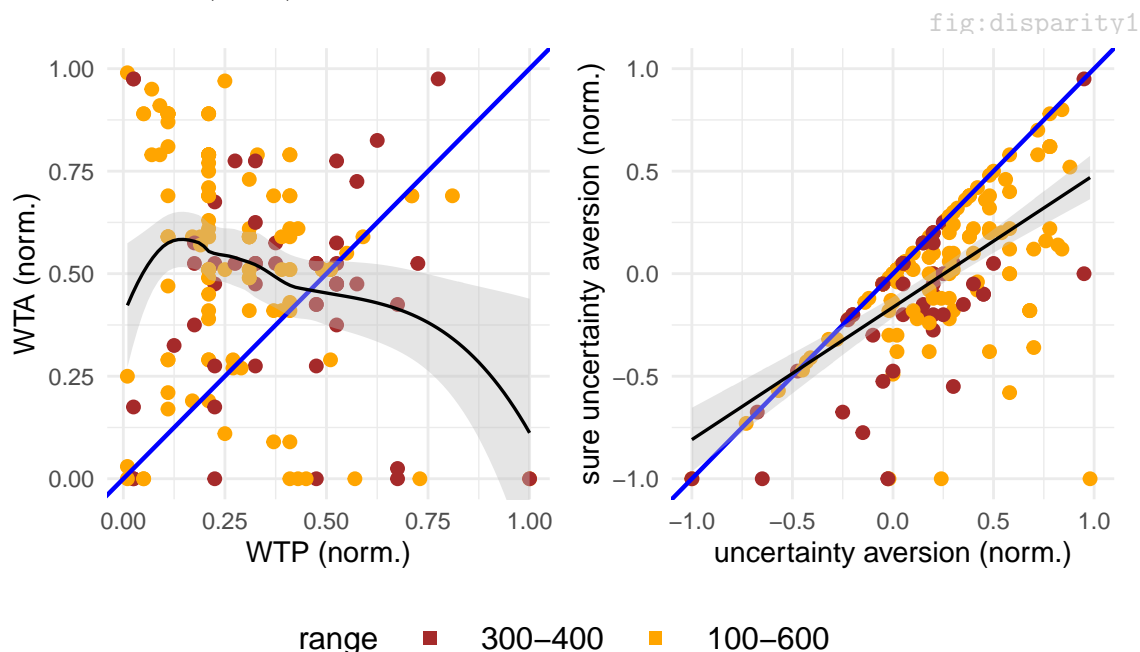


fig:absolutedecomp

Figure 7: Left panel: association between WTA and WTP (both normalized by subtracting minimal pay-off and dividing by pay-off range). LOESS regression line added. Right panel: association between uncertainty aversion and sure uncertainty aversion (both normalized by dividing by pay-off range). Regression line added. Both axes clipped to $(-1, 1)$.



effect and therefore treat WTA as the selling price of an initially owned object. However, under their assumption that the (stochastic) status quo serves as the reference point, there is no difference between the selling and short-selling prices. Second, our domain consists of prospects (Savage acts mapping states to payoffs), whereas their domain consists of lotteries over bundles. We can therefore model ambiguity, while their model captures trade-offs between goods in a risk setting. Third, our approach is model-independent,¹⁵ whereas Cerreia-Vioglio et al. (2024) derive the existence of the WTA–WTP gap and loss aversion for risk from their (symmetric) cautious utility representation. By contrast, we *characterize* the WTA–WTP gap and loss aversion axiomatically. Finally, while Cerreia-Vioglio et al. (2024) show that loss aversion and the WTA–WTP gap are not necessarily related (neither implies the other, even under

¹⁵For example, the definitions of short-selling and buying prices are robust to changes in reference-point determination rules (Lewandowski and Woźny, 2022).

cautious expected utility), in our setting the WTA–WTP gap implies loss aversion, but the reverse implication requires additional structure and assumptions.

WTA-WTP disparity in the cautious completion of the MUMP model

Assume \succsim has a MUMP representation with the set of priors and utilities is Φ . We may consider a cautious completion of \succsim denoted by \succsim^* on \mathcal{F} defined as follows: for any $f, g \in \mathcal{F}$, $f \succsim^* g \iff \min_{(\mu, u) \in \Phi} u^{-1} \left(\int_S u(f) d\mu \right) \geq \min_{(\mu, u) \in \Phi} u^{-1} \left(\int_S u(g) d\mu \right)$. Hara and Riella (2023)¹⁶ suggests the following interpretation: \succsim represents choices that can be made with certainty, while \succsim^* represents forced choices that are made even if the DM is not confident. Under \succsim^* we have the following observation for any $f \in \mathcal{F}$: $B(f) = B_n(f) = \min_{(\mu, u) \in \Phi} B_{\mu, u}(f)$ and $B^*(f) = B_n^*(f) = \max_{(\mu, u) \in \Phi} B_{\mu, u}^*(f)$. The above is a simple counterpart of Proposition 4 for \succsim^* .

Incentive problems in experimental design Incentive-compatible elicitation procedures are standard in experimental economics, typically implemented by (randomized) monetary payoffs based on elicited preferences. In our setting, however, two difficulties arise. First, it is unclear how to incentivize the elicitation of loss aversion. Our framework compares the prices of f and $-f$, and at least one of these prospects involves negative payoffs. For truthful revelation, participants must treat such losses as real possibilities, which conflicts with the usual requirement that participants should not lose money. Previous studies attempted to address this by introducing upfront payments (e.g., show-up fees) that are reduced if a “negative prize” is drawn (e.g., Schmidt and Traub, 2002; Abdellaoui et al., 2007). However, this approach is limited by the size of the show-up fee, especially when one wishes to study substantial losses. Second, it is unclear how to incentivize choices in regions of indecision or preference incompleteness. The “I am not sure” region does not correspond to a definite action, making it difficult to design payoffs that induce truthful revelation of no-buying or no-short-selling prices. In particular, distinguishing “surely no buying” from “not buy-

¹⁶See also Gilboa et al. (2010).

ing out of caution” is challenging. One possible solution is to delegate the decision in the imprecision region to an external DM with complete preferences; see Cettolin and Riedl (2019); Nielsen and Rigotti (2024) for recent discussions. Finally, the literature has begun to distinguish incompleteness from indifference regions, and some progress has been made (e.g., Agranov and Ortoleva, 2025).

8 Proofs

S:proofs

Proof of Lemma 1 Take any $f \in \mathcal{F}$. We prove all statements for $B(f)$. The remaining cases are proved similar. We first show existence. If $f = \theta^*$ for some $\theta^* \in \mathbb{R}$ then by **B0–B1** $B(f) = \theta^* = \underline{f} = \bar{f}$. Assume that f is nonconstant and define: $\mathcal{B}(f) := \{\theta \in \mathbb{R} : f - \theta \succcurlyeq 0\}$, $A := \{g \in \mathcal{F} : g = f - \theta, \theta \in \mathbb{R}\}$, $A' := \{g \in \mathcal{F} : g = f - \theta, \theta \in \mathcal{B}(f)\}$. We first show that $\mathcal{B}(f)$ is nonempty. Indeed it contains \underline{f} : $f - \underline{f} \geq 0$ and $f \neq \underline{f}$, which, in view of **B1**, implies $f - \underline{f} \succ 0$. Hence, $\underline{f} \in \mathcal{B}(f)$. We now show that $\mathcal{B}(f)$ is bounded from above. Indeed since $f - \theta \leq 0$, $f \neq \theta$, for $\theta \geq \bar{f}$, so by **B1** $0 \succ f - \theta$ which implies that $f - \theta \not\succcurlyeq 0$. So $\mathcal{B}(f)$ does not contain any $\theta \geq \bar{f}$. We next show that $\mathcal{B}(f)$ is closed. A' is the intersection of A , which is closed, and nW, which is also closed by **B2**. So A' is also closed. Define a function $\gamma : \mathbb{R} \rightarrow \mathcal{F}$ by $\gamma(\theta) = f - \theta$. Note that γ is a continuous function. Hence a preimage of any closed set is closed. Note that a preimage of A' is $\mathcal{B}(f)$, and since the former is closed, the latter must also be. We have shown that $\mathcal{B}(f)$ is a nonempty and closed set bounded from above. So $\mathcal{B}(f)$ contains its maximum, which proves that $B(f)$ exists. It is also unique by monotonicity.

We now prove that $B(f) \in [\underline{f}, \bar{f}]$. We have already shown that $\underline{f} \in \mathcal{B}(f)$ so by the definition of the latter $B(f) \geq \underline{f}$. Now observe that $f - \bar{f} \leq 0$, $f \neq \bar{f}$, so **B1** implies that $0 \succ f - \bar{f}$. On the other hand $f - B(f) \succcurlyeq 0$. By **B0**, $f - B(f) \succcurlyeq f - \bar{f}$. By **B1** we must have $\bar{f} \geq B(f)$ which finishes the proof of (i).

We now show $B_n(f) \geq B(f)$. By definition $f - B(f) \succcurlyeq 0$ and $0 \succcurlyeq f - B_n(f)$. So by

614 **B0**, $f - B(f) \succsim f - B_n(f)$. By **B1** we have $B_n(f) \geq B(f)$.

615 We now prove the last statement. Suppose that for some prospect f one of the
 616 inequalities in (5) are strict, say $B_n(f) > B(f)$. To show that preferences are incom-
 617 plete, it suffices to show that there is a pair of noncomparable prospects. Take $\theta \in \mathbb{R}$
 618 such that $B_n(f) > \theta > B(f)$. By the definition of $B(f)$, $f - \theta \not\succsim 0$. By the definition
 619 of $B_n(f)$, $0 \not\succsim f - \theta$. So 0 and $f - \theta$ are not comparable and \succsim is incomplete.

Proof of Lemma 2 We show that for $X \in \{B^*, B, B_n^*, B_n\}$ it holds: $X(f + \lambda) = X(f) + \lambda$ for any $\lambda \in \mathbb{R}$, $f \in \mathcal{F}$. We show it for $X = B$. The rest is analogous:

$$B(f + \lambda) = \max\{\theta \in \mathbb{R} : f + \lambda - \theta \succsim 0\} = \lambda + \max\{\theta \in \mathbb{R} : f - \theta \succsim 0\}.$$

620 Moreover, for all $f \in \mathcal{F}$, the following holds: $B(-f) = -B^*(f)$. Indeed:

$$\begin{aligned} -B(-f) &= -\max\{\theta \in \mathbb{R} : -f - \theta \succsim 0\} = \min\{-\theta \in \mathbb{R} : -\theta - f \succsim 0\} = \\ &= \min\{\theta' \in \mathbb{R} : \theta' - f \succsim 0\} = B^*(f). \end{aligned}$$

621 Hence $B^*(f) = -B(-f) = \theta - B(\theta - f)$ and thus the first equation of (6) holds.
 622 Similarly, the second equation holds because B_n is translation invariant and, for all
 623 $f \in \mathcal{F}$, $B_n(-f) = -B_n^*(f)$.

624 **Proof of Theorem 1** Suppose that UA holds. By the definition of B , for any
 625 nonzero prospect f , $f - B(f) \succsim 0$. UA implies that $B(f) - f \not\succsim 0$, which in view
 626 of the definition of B^* implies that $B(f) < B^*(f)$. Now assume that $B^*(f) > B(f)$
 627 for some nonzero prospect f such that $f \succsim 0$. We must prove that $-f \not\succsim 0$. By the
 628 definition of B and in view of the monotonicity of \succsim , we have $B(f) \geq 0$ and thus
 629 $B^*(f) > 0$. From the definition of B^* , we obtain that $-f \not\succsim 0$.

630 **Proof of Theorem 3** We only prove the first part, as the second part follows similar
 631 reasoning. Suppose that the DM is imprecise with respect to f . Then there is a $\theta \in \mathbb{R}$
 632 such that $f + \theta \not\succsim 0$ and $0 \not\succsim f + \theta$. By the definition of B , $-\theta > B(f)$. Similarly,
 633 by the definition of B_n , $B_n(f) > -\theta$. It follows that $B_n(f) > B(f)$. Similarly, if

634 $B_n(f) > B(f)$ holds for some prospect f , take $\theta \in \mathbb{R}$ such that $B_n(f) > -\theta > B(f)$.
635 By the definition of B and B_n , it holds: $f + \theta \not\geq 0$ and $0 \not\geq f + \theta$.

636 **Proof of Theorem 4** We first prove the \Rightarrow part. Assume that sure UA holds and
637 suppose, by way of contradiction, that for some nonzero prospect f , $B^*(f) \leq B(f)$
638 or $B_n^*(f) < B_n(f)$. If $B^*(f) \leq B(f)$, then take $\theta \in \mathbb{R}$ such that $B^*(f) \leq \theta \leq B(f)$.
639 By the definitions of B^* and B , this implies that $f - \theta \succ 0$ and $\theta - f \succ 0$, which
640 implies that $0 \not\geq f - \theta$ and $0 \not\geq \theta - f$, a contradiction to sure UA. If $B_n^*(f) < B_n(f)$,
641 then take $\theta \in \mathbb{R}$ such that $B_n^*(f) < \theta < B_n(f)$. By the definitions of B_n and B_n^* , we
642 have $0 \not\geq f - \theta$ and $0 \not\geq \theta - f$. This implies $0 \not\geq f - \theta$ and $0 \not\geq \theta - f$, a contradiction
643 to sure UA. This finishes this part of the proof.

644 We now prove the \Leftarrow part. We assume that for any nonzero prospect f , $B^*(f) > B(f)$
645 and $B_n^*(f) \geq B_n(f)$. We take an arbitrary nonzero prospect f such that $0 \not\geq f$. This
646 means that $0 \not\geq f$ or $f \succ 0$. If $0 \not\geq f$, then, by the definition of B_n , $B_n(f) > 0$.
647 Hence $B_n^*(f) > 0$ and $B^*(f) > 0$, by assumption. In view of the definitions of B_n^*
648 and B^* , we obtain $0 \succ -f$ and $-f \not\geq 0$ which implies $0 \succ -f$. If $f \succ 0$, then, by the
649 definition of B , $B(f) \geq 0$, so, by assumption, $B^*(f) > 0$ and $B_n^*(f) \geq 0$. In view of
650 the definitions of B^* and B_n^* , we obtain $-f \not\geq 0$ and $0 \succ -f$, which implies $0 \succ -f$.

651 **Proof of Theorem 5** Suppose that strong UA holds and consider an arbitrary
652 nonzero prospect f . By the definition of B , $f - B(f) \succ 0$, which implies, by strong
653 UA, $0 \succ B(f) - f$ which means $0 \succ B(f) - f$ and $B(f) - f \not\geq 0$. By the definition
654 of B_n^* and B^* , these imply $B_n^*(f) \geq B(f)$ and $B^*(f) > B(f)$. As f is arbitrary,
655 the same holds for $-f$ and hence, in view of Lemma 2 (applied for $\theta = 0$), we have
656 $-B_n(f) \geq -B^*(f)$ and conclude that $B^*(f) \geq B_n(f)$. This finishes the proof of the
657 first part of the proposition. To prove the converse, we take an arbitrary nonzero
658 prospect f and assume that $B_n^*(f) \geq B(f)$ and $B^*(f) > B(f)$ holds. We also assume
659 that $f \succ 0$. This, by the definition of B implies that $B(f) \geq 0$. By our assumptions
660 it implies that $B^*(f) > 0$ and $B_n^*(f) \geq 0$ and, by the definitions of B^* and B_n^* , implies
661 that $0 \succ -f$ and $-f \not\geq 0$, which implies $0 \succ -f$. This completes the proof.

Proof of Proposition 1 Let A, A^c be symmetric events and let $x, y \in \mathbb{R}$. By the definition of B , $(x - B(x, y; A), y - B(x, y; A); A) \succsim 0$. Because A, A^c are symmetric, $(y - B(x, y; A), x - B(x, y; A); A) \succsim 0$. By the definition of B , $B(y, x; A) \geq B(x, y; A)$. Repeating the same argument with $B(y, x; A)$ instead of $B(x, y; A)$ shows that $B(x, y; A) \geq B(y, x; A)$, which together with the previous inequality yields $B(x, y; A) = B(y, x; A)$. Similarly, one can show that $B_n(x, y; A) = B_n(y, x; A)$. Applying Lemma 2 (with $\theta = x + y$) and the already proved part, we get $B^*(x, y; A) - B_n^*(x, y; A) = x + y - B(y, x; A) - x - y + B_n(y, x; A) = B_n(x, y; A) - B(x, y; A)$.

Proof of Proposition 2 Assume \succsim has a SEU representation with utility u and probability μ . We first prove that if (A, A^c) are symmetric events then $\mu(A) = \frac{1}{2} = \mu(A^c)$. Indeed, by the definition of symmetric events, for any $x, y \in X$, $(x, y; A) \sim (y, x; A)$. By the definition of SEU, this is equivalent to $\mu(A)u(x) + (1 - \mu(A))u(y) = \mu(A)u(y) + (1 - \mu(A))u(x)$ or $(u(x) - u(y))(2\mu(A) - 1) = 0$, and since u is strictly increasing, $\mu(A) = \frac{1}{2}$. We now prove that \succsim is loss averse if and only if $u(x) < -u(-x)$ for all $x \in X \setminus \{0\}$. Take arbitrary symmetric events (A, A^c) and an arbitrary $x \in X \setminus \{0\}$. By the definition of LA, $0 \succ (x, -x; A)$, or equivalently $0 \succsim (x, -x; A)$ and $0 \not\succ (x, -x; A)$. By SEU and the fact that $\mu(A) = \frac{1}{2}$, this is equivalent to $\frac{1}{2}u(x) + \frac{1}{2}u(-x) < u(0) = 0$ or $u(x) < -u(-x)$ for all $x \in X \setminus \{0\}$.

SEU preferences are complete. Hence, LA and not-LL are equivalent and so are different notions of uncertainty aversion: UA, strong UA and sure UA. In view of Theorem 6 (proved below), it suffices to show that LA implies UA. Assume \succsim is loss averse and $f \succsim 0$ for some nonzero f . By SEU, $\int_S u(f)d\mu \geq 0$. By loss aversion, $u(x) < -u(-x)$ for all $x \in X \setminus \{0\}$ and hence $\int_S u(-f)d\mu < 0$. By SEU $-f \not\succ 0$ and hence UA holds. The proof that \succsim is uncertainty neutral if and only if u is odd follows similar logic and hence is omitted.

Proof of Theorem 6 Assume that \succsim is surely uncertainty averse. It implies that for any nonzero prospect f , $0 \succ f$ or $0 \succ -f$. Take any $x \neq 0$ and a pair of symmetric events (A, A^c) . Set $f = (x, -x; A)$. Then $-f = (-x, x; A)$ and by the

definition of symmetric events $f \sim -f$. By transitivity (**B0**), $0 \succcurlyeq f \iff 0 \succcurlyeq -f$ and $f \not\succcurlyeq 0 \iff -f \not\succcurlyeq 0$. Hence $0 \succ f \iff 0 \succ -f$ and therefore $0 \succ f$ and $0 \succ -f$. Since $-f = (-x, x; A) = (x, -x; A^c)$, we have proved that $0 \succ (x, -x; A)$ and $0 \succ (x, -x; A^c)$. Because x and A were arbitrary, the proof of the first implication is completed. The proof of the second implication is similar. The only difference is that by transitivity, if $f \sim -f$, then $f \not\succcurlyeq 0 \iff -f \not\succcurlyeq 0$.

Proof of Theorem 7 We prove (i). First note that for any f, g we must have $f \not\succcurlyeq g$ or $g \not\succcurlyeq f$: otherwise $f \succ g$ and $g \succ f$, which by definition of \succ would imply both $f \succcurlyeq g$ and $f \not\succcurlyeq g$, a contradiction. For any purely subjective act f , let $-f$ be the act assigning to each state the negative of the payoff assigned by f . Then either $f \not\succcurlyeq -f$ or $f \succcurlyeq -f$. Suppose $f \not\succcurlyeq -f$. By SUA, $\frac{1}{2}f + \frac{1}{2}(-f) \succcurlyeq -f$. Recall that the expression $\frac{1}{2}f(s) + \frac{1}{2}(-f(s))$ denotes the constant act delivering the lottery $\frac{1}{2}f(s) + \frac{1}{2}(-f(s))$ in every state. Not-LL implies $\frac{1}{2}f(s) + \frac{1}{2}(-f(s)) \not\succcurlyeq 0$ for all s , and by the additional monotonicity condition we obtain $\frac{1}{2}f + \frac{1}{2}(-f) \not\succcurlyeq 0$. We claim that $-f \not\succcurlyeq 0$: otherwise $-f \succcurlyeq 0$ would contradict the previous conclusion or transitivity. The symmetric case $f \not\succcurlyeq -f$ yields $f \not\succcurlyeq 0$. Thus, for any f , either $f \not\succcurlyeq 0$ or $-f \not\succcurlyeq 0$, completing the proof of (i). The proof of (ii) is analogous and omitted.

Proof of Theorem 8 and 9 We prove only (i) of Theorem 8; proofs of part (ii) and Theorem 9 are analogous. For the “only if” direction, take any nonzero prospect f . By the definitions of B_1 and B_1^* , agent 1 prefers both $f - B_1(f)$ and $B_1^*(f) - f$ to the status quo. Let $\epsilon := B_1^*(f) - B_1(f)$. If agent 1 is more uncertainty averse than agent 2, then there exists $\delta \in \mathbb{R}$ such that $f - B_1(f) - \delta \succcurlyeq_2 0$ and $\delta + B_1^*(f) - f \succcurlyeq_2 0$. By the definitions of B_2 and B_2^* , this implies $B_1(f) + \delta \leq B_2(f)$ and $\delta + B_1^*(f) \geq B_2^*(f)$. Hence $B_1^*(f) - B_1(f) \geq B_2^*(f) - B_2(f)$. Since f was arbitrary, this completes the “only if” part. For the “if” part, assume the antecedent. We must show that agent 1 is more uncertainty averse than agent 2. Take any f and $\epsilon \in \mathbb{R}$ such that $f \succcurlyeq_1 0$ and $\epsilon - f \succcurlyeq_1 0$. By the definitions of B_1, B_1^* , we have $B_1(f) \geq 0$, $B_1^*(f) \leq \epsilon$, hence $B_1^*(f) - B_1(f) \leq \epsilon$. By assumption, $B_2^*(f) - B_2(f) \leq \epsilon$ (*). By

the definition of B_2 , $f - B_2(f) \succsim_2 0$. Let $\delta := B_2(f)$, so $f - \delta \succsim_2 0$. From (*),
 $B_2^*(f) = B_2(f) + (B_2^*(f) - B_2(f)) \leq \delta + \epsilon$, and by the definition of B_2^* this means
 $\delta + \epsilon - f \succsim_2 0$. Since f was arbitrary, the proof is complete.

Proof of Theorem 2 We first prove the “only if” part. Take an arbitrary prospect
 f . For an UA neutral DM there is a unique scalar θ^* such that $f - \theta^* \succsim 0$ and
 $\theta^* - f \succsim 0$. Note that for all $\theta \geq \theta^*$, $\theta - f \succsim 0$ by monotonicity (B1). By uniqueness
of θ^* , it follows that $f - \theta \not\succsim 0$. Hence, by the definition of B , $\theta^* = B(f)$. Similarly,
for all $\theta \leq \theta^*$, $f - \theta \succsim 0$ and $\theta - f \not\succsim 0$, and hence, in view of the definition of B^* ,
 $\theta^* = B^*(f)$. So $B^*(f) - B(f) = 0$. We now prove the converse. Take an arbitrary
prospect f . Define $\theta^* := B(f)$. By assumption, $\theta^* = B^*(f)$. By Lemma 1, such θ^*
is unique. By the definition of B and B^* , it follows that $f - \theta^* \succsim 0$ and $\theta^* - f \succsim 0$.
Furthermore, there is no other θ satisfying these conditions, because for all $\theta < \theta^*$,
 $\theta - f \not\succsim 0$ and for all $\theta > \theta^*$, $f - \theta \not\succsim 0$.

Proof of Theorem 10 We need to prove that each of the two, (i) and (ii), implies
that (13)–(14) hold whenever g is more uncertain than f . As the proofs in the two
cases, (i) and (ii), are very similar, we will proceed with one proof and highlight the
differences in the two cases. Take two prospects f, g such that g is more uncertain
than f , i.e., $h := g - f$ is a nonconstant prospect comonotonic with f . We observe
that, for any $\theta \in \mathbb{R}$, the prospect $g - B_n(f) - \theta$ is more uncertain than $f - B_n(f)$,
and their difference is given by $g - B_n(f) - \theta - (f - B_n(f)) = h - \theta$. Similarly, since
 $-g$ is more uncertain than $-f$ whenever g is more uncertain than f , we note that,
for any $\theta \in \mathbb{R}$, the prospect $B_n^*(f) + \theta - g$ is more uncertain than $B_n^*(f) - f$, and
their difference is $B_n^*(f) + \theta - g - (B_n^*(f) - f) = \theta - h$. Hence, for θ in the set

$$\{\theta \in \mathbb{R} : h - \theta \not\succsim 0 \wedge \theta - h \not\succsim 0\}, \quad \text{Eq: 1220-5 (23)}$$

prospect $f - B_n(f)$ uncertainty-dominates $g - B_n(f) - \theta$ and prospect $B_n^*(f) - f$

742 uncertainty-dominates $B_n^*(f) + \theta - g$. Similarly, for θ in the set

$$\{\theta \in \mathbb{R} : h - \theta \not\asymp 0 \wedge \theta - h \not\asymp 0\}, \quad \text{Eq: 1220-6} \quad (24)$$

743 prospect $f - B_n(f)$ strongly uncertainty-dominates $g - B_n(f) - \theta$ and prospect $B_n^*(f) -$
 744 f strongly uncertainty-dominates $B_n^*(f) + \theta - g$. So, for θ in the corresponding set and
 745 monotonicity with respect to the corresponding dominance, uncertainty-dominance
 746 in the case of (i) and strong-uncertainty dominance in the case of (ii), would imply
 747 $f - B_n(f) \succcurlyeq g - B_n(f) - \theta$ and $B_n^*(f) - f \succcurlyeq B_n^*(f) + \theta - g$, which in view of the
 748 definitions of $B_n(f)$ and $B_n^*(f)$ as well as transitivity of \succcurlyeq , yields $0 \succcurlyeq g - B_n(f) - \theta$ and
 749 $0 \succcurlyeq B_n^*(f) + \theta - g$. By the definitions of $B_n(g)$ and $B_n^*(g)$, we get $B_n(g) \leq B_n(f) + \theta$
 750 and $B_n^*(g) \geq B_n^*(f) + \theta$, or, after combining the two inequalities, $B_n^*(g) - B_n(g) \geq$
 751 $B_n^*(f) - B_n(f)$. So, in order to prove that (14) is implied by (i), respectively (ii), we
 752 need to show that the set defined by (23), respectively by (24), is nonempty.

753 Similarly, we observe that for any $\theta \in \mathbb{R}$, prospect $g - B(g)$ is more uncertain than
 754 $f + \theta - B(g)$ and their difference is given by $g - B(g) - (f + \theta - B(g)) = h -$
 755 θ . Moreover, prospect $B^*(g) - g$ is more uncertain than $B^*(g) - \theta - f$ and their
 756 difference is $B^*(g) - g - (B^*(g) - \theta - f) = \theta - h$. So for θ in the set defined by (23),
 757 prospect $f + \theta - B(g)$ uncertainty-dominates $g - B(g)$ and prospect $B^*(g) - \theta - f$
 758 uncertainty-dominates $B^*(g) - g$. Similarly, for θ in the set defined by (24), prospect
 759 $f + \theta - B(g)$ strongly uncertainty-dominates $g - B(g)$ and prospect $B^*(g) - \theta - f$
 760 strongly uncertainty-dominates $B^*(g) - g$. So, for θ in the corresponding set and
 761 monotonicity with respect to the corresponding dominance, uncertainty-dominance
 762 in the case of (i) and strong-uncertainty dominance in the case of (ii), would imply
 763 $f + \theta - B(g) \succcurlyeq g - B(g)$ and $B^*(g) - \theta - f \succcurlyeq B^*(g) - g$, which in view of the
 764 definitions of $B(f)$ and $B^*(f)$ as well as transitivity of \succcurlyeq , yields $f + \theta - B(g) \succcurlyeq 0$
 765 and $B^*(g) - \theta - f \succcurlyeq 0$. By the definitions of $B(g)$ and $B^*(g)$, we would thus get
 766 $B(f) \geq B(g) - \theta$ and $B^*(f) \leq B^*(g) - \theta$, or, after combining the two inequalities,
 767 $B^*(g) - B(g) \geq B^*(f) - B(f)$.

So, in order to prove that (13) is implied by (i), respectively (ii), we need to show that the set (23), respectively (24), is nonempty. In the case (i), \succsim satisfies sure UA. Theorem 4 implies $B_n^*(h) \geq B_n(h)$ and so, there is $\theta \in \mathbb{R}$ such that $B_n(h) \leq \theta \leq B_n^*(h)$. By the definitions of B_n^* and B_n , $0 \succsim h - \theta$ and $0 \succsim \theta - h$, and hence we have $h - \theta \not\succ 0$ and $\theta - h \not\succ 0$. This proves that the set defined by (23) is nonempty. In the case (ii), \succsim satisfies UA. Theorem 1 implies that $B^*(h) > B(h)$ and so, there is $\theta \in \mathbb{R}$ such that $B(h) < \theta < B^*(h)$. By the definitions of B^* and B , $h - \theta \not\succ 0$ and $\theta - h \not\succ 0$. This proves that the set defined by (24) is nonempty and finishes the proof.

Proof of Theorem 11 Let $B_1 := B(x, y; F)$ and $B_1^* := B^*(x, y; F)$. If (E, E^c) dominates (F, F^c) , then $(x - B_1, y - B_1; E) \succsim (x - B_1, y - B_1; F) \succsim 0$, where the last inequality follows from the definition of B_1 . By transitivity, $(x - B_1, y - B_1; E) \succsim 0$. Hence, by the definition of B , we have $B(x, y; E) \geq B_1 = B(x, y; F)$. Similarly, $(B_1^* - y, B_1^* - x; E^c) \succsim (B_1^* - y, B_1^* - x; F^c) = (B_1^* - x, B_1^* - y; F) \succsim 0$, where the last inequality follows from the definition of B_1^* . By transitivity, $(B_1^* - x, B_1^* - y; E) = (B_1^* - y, B_1^* - x; E^c) \succsim 0$. Hence, by the definition of B^* , we have $B^*(x, y; E) \leq B_1^* = B^*(x, y; F)$. So we obtain $B^*(x, y; E) - B(x, y; E) \leq B^*(x, y; F) - B(x, y; F)$, which proves the first part of the Theorem.

Suppose now that one of the preferences, say the first one, in (15) is strict. Then following similar reasoning as above yields $B_n(x, y; E) > B_1 = B(x, y; F)$. We also know from the previous part of the proof that $B^*(x, y; E) \leq B^*(x, y; F)$. In view of Theorem 3, we have $B_n^*(x, y; E) \leq B^*(x, y; E)$. Hence $B_n^*(x, y; E) - B_n(x, y; E) \leq B^*(x, y; E) - B_n(x, y; E) < B^*(x, y; F) - B(x, y; F)$, which completes the proof.

Proof of Proposition 4 We only prove it for B as the rest is similar. Take an arbitrary $f \in \mathcal{F}$. We can rewrite the definition of B as follows

$$B(f) = \max \left\{ \theta \in \mathbb{R} : \sum_{s \in S} \mu(s) u(f(s) - \theta) \geq 0 \text{ for all } (\mu, u) \in \Phi \right\}. \quad \text{Eq: 1030-3} \quad (25)$$

791 We will prove that $B(f) = \hat{\theta} := \min_{(\mu, u) \in \Phi} B_{\mu, u}(f)$. Note that

$$\sum_{s \in S} \mu(s) u(f(s) - \hat{\theta}) \geq 0 \quad \text{for all } (\mu, u) \in \Phi. \quad \text{Eq:1030-7} \quad (26)$$

792 Hence, by (25), $B(f) \geq \hat{\theta}$. Suppose that $\theta' > \hat{\theta}$ and let

$$(\mu^*, u^*) := \arg \min_{(\mu, u) \in \Phi} B_{\mu, u}(f). \quad \text{Eq:1030-9} \quad (27)$$

793 Then, by monotonicity $\sum_{s \in S} \mu^*(s) u^*(f(s) - \theta') < 0$, but this, in view of (25), implies
794 that $\theta' \neq B(f)$. So it must be that $B(f) = \hat{\theta}$.

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